

Attribution-based Explanations that Provide Recourse Cannot be Robust

Joint work with
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Programme of today

- ▶ Brief introduction to Explainable Artificial Intelligence
- ▶ Attribution Methods
- ▶ Recourse and Robustness
- ▶ Impossibility result
- ▶ When Recourse is possible

Explainable Artificial intelligence (XAI)

Interpretable Machine Learning (IML)

Call for XAI

Some Reasons

- ▶ Fairness: Biases can be detected earlier
- ▶ Trustworthiness
- ▶ Increases reliability
- ▶ Regulation

GDPR
General Data Protection
Regulation



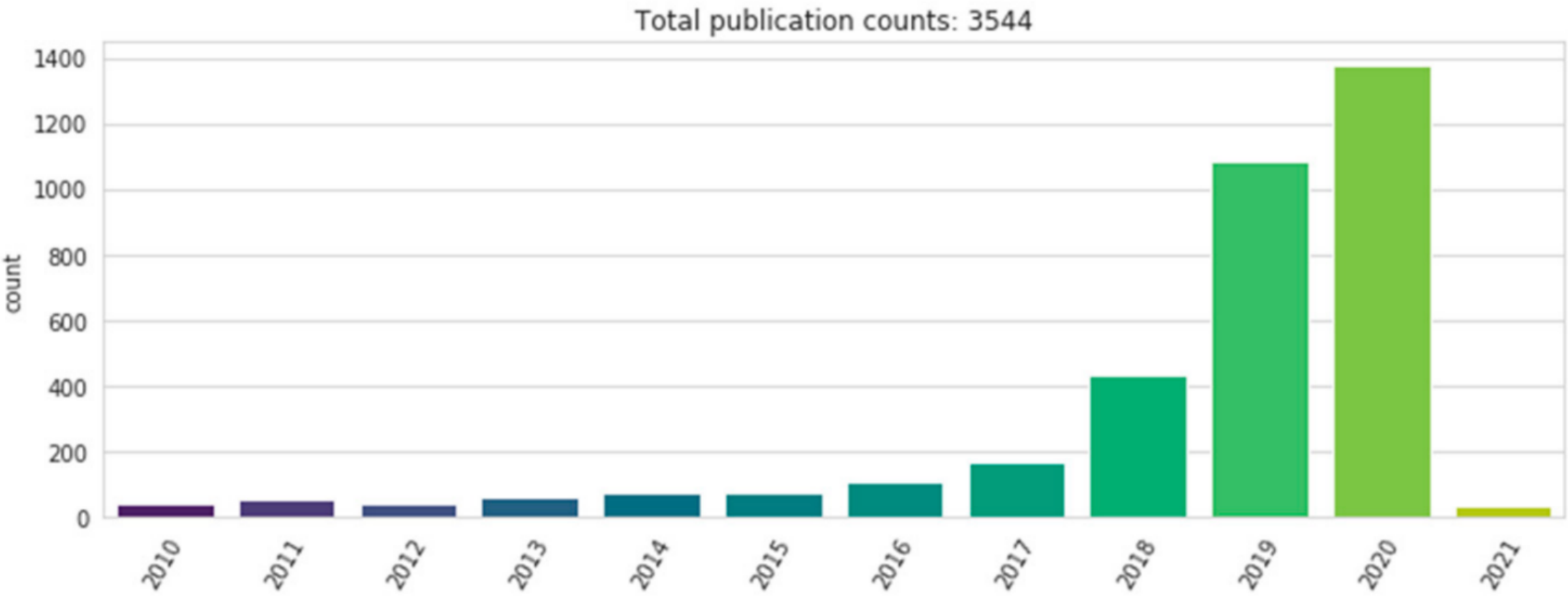
Explanations

Explosion

Methods
CAM with global average pooling [42], [91] + Grad-CAM [43] generalizes CAM, utilizing gradient + Guided Grad-CAM and Feature Occlusion [68] + Respond CAM [44] + Multi-layer CAM [92] LRP (Layer-wise Relevance Propagation) [13], [53] + Image classifications. PASCAL VOC 2009 etc [45] + Audio classification. AudioMNIST [47] + LRP on DeepLight. fMRI data from Human Connectome Project [48] + LRP on CNN and on BoW(bag of words)/SVM [49] + LRP on compressed domain action recognition algorithm [50] + LRP on video deep learning, <i>selective relevance method</i> [52] + BiLRP [51] DeepLIFT [57] Prediction Difference Analysis [58] Slot Activation Vectors [41] PRM (Peak Response Mapping) [59]
LIME (Local Interpretable Model-agnostic Explanations) [14] + MUSE with LIME [85] + Guidelinebased Additive eXplanation optimizes complexity, similar to LIME [93] # Also listed elsewhere: [56], [69], [71], [94]
Others. Also listed elsewhere: [95] + Direct output labels. Training NN via multiple instance learning [65] + Image corruption and testing Region of Interest statistically [66] + Attention map with autofocus convolutional layer [67]
DeconvNet [72] Inverting representation with natural image prior [73] Inversion using CNN [74] Guided backpropagation [75], [91]
Activation maximization/optimization [38] + Activation maximization on DBN (Deep Belief Network) [76] + Activation maximization, multifaceted feature visualization [77] Visualization via regularized optimization [78] Semantic dictionary [39]
Network dissection [36], [37]
Decision trees Propositional logic, rule-based [82] Sparse decision list [83] Decision sets, rule sets [84], [85] Encoder-generator framework [86] Filter Attribute Probability Density Function [87] MUSE (Model Understanding through Subspace Explanations) [85]

(2014.03) SEDC [129]
(2015.08) OAE [51]
(2016.05) HCLS [110, 112]
(2017.06) Feature Tweaking [186]
(2017.11) CF Expl. [196]
(2017.12) Growing Spheres [114]
(2018.02) CEM [55]
(2018.02) POLARIS [209]
(2018.05) LORE [80]
(2018.06) Local Foil Trees [190]
(2018.09) Actionable Recourse [189]
(2018.11) Weighted CFs [77]
(2019.01) Efficient Search [175]
(2019.04) CF Visual Expl. [76]
(2019.05) MACE [99]
(2019.05) DiCE [145]
(2019.05) CERTIFAI [179]
(2019.06) MACEM [56]
(2019.06) Expl. using SHAP [165]
(2019.07) Nearest Observable [201]
(2019.07) Guided Prototypes [191]
(2019.07) REVISE [95]
(2019.08) CLEAR [202]
(2019.08) MC-BRP [123]
(2019.09) FACE [162]
(2019.09) Equalizing Recourse [83]
(2019.10) Action Sequences [163]
(2019.10) C-CHVAE [156]
(2019.11) FOCUS [124]
(2019.12) Model-based CFs [127]
(2019.12) LIME-C/SHAP-C [164]
(2019.12) EMAP [41]
(2019.12) PRINCE [71]
(2019.12) LowProFool [18]
(2020.01) ABELE [79]
(2020.01) SHAP-based CFs [66]
(2020.02) CEML [11–13]
(2020.02) MINT [100]
(2020.03) ViCE [74]
(2020.03) Plausible CFs [22]
(2020.04) SEDC-T [193]
(2020.04) MOC [52]
(2020.04) SCOUT [199]
(2020.04) ASP-based CFs [28]
(2020.05) CBR-based CFs [103]
(2020.06) Survival Model CFs [106]
(2020.06) Probabilistic Recourse [101]
(2020.06) C-CHVAE [155]
(2020.07) FRACE [210]
(2020.07) DACE [96]
(2020.07) CRUDS [60]
(2020.07) Gradient Boosted CFs [5]
(2020.08) Gradual Construction [97]
(2020.08) DECE [44]
(2020.08) Time Series CFs [16]
(2020.08) PermuteAttack [87]
(2020.10) Fair Causal Recourse [195]
(2020.10) Recourse Summaries [167]
(2020.10) Strategic Recourse [43]
(2020.11) PARE [172]

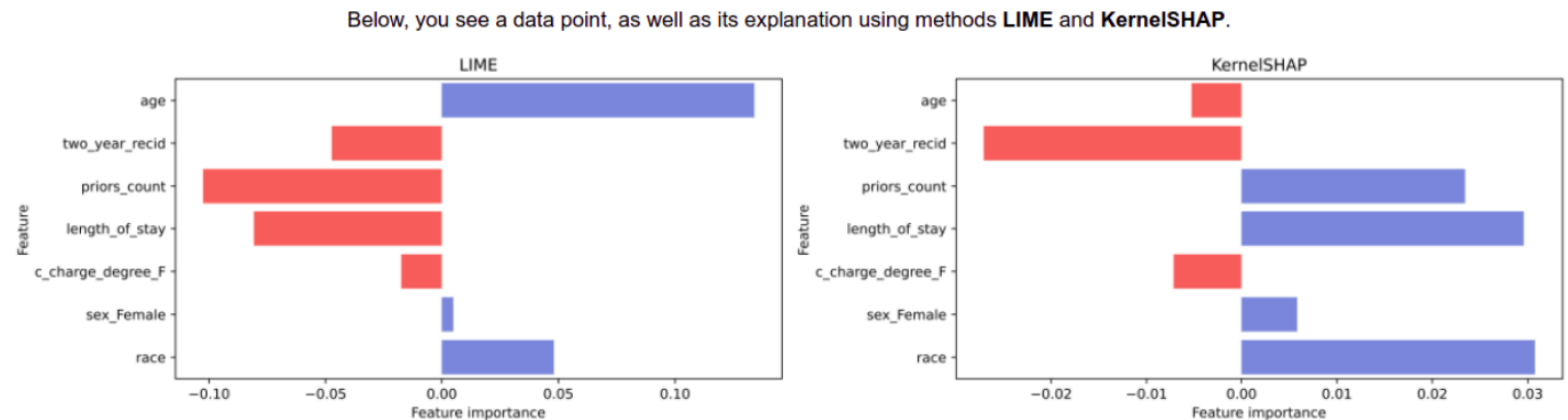
Methods	H
Linear probe [101]	,
Regression based on CNN [106]	,
Backwards model for interpretability of linear models [107]	,
GDM (Generative Discriminative Models): ridge regression + least square [100]	,
GAM, GA ² M (Generative Additive Model) [82], [102], [103]	,
ProtoAttend [105]	,
Other content-subject-specific models:	N
+ Kinetic model for CBF (cerebral blood flow) [131]	N
+ CNN for PK (Pharmacokinetic) modelling [132]	N
+ CNN for brain midline shift detection [133]	N
+ Group-driven RL (reinforcement learning) on personalized healthcare [134]	N
+ Also see [108]–[112]	N
PCA (Principal Components Analysis), SVD (Singular Value Decomposition)	N
CCA (Canonical Correlation Analysis) [113]	,
SVCCA (Singular Vector Canonical Correlation Analysis) [97] = CCA+SVD	,
F-SVD (Frame Singular Value Decomposition) [114] on electromyography data	,
DWT (Discrete Wavelet Transform) + Neural Network [135]	,
MODWPT (Maximal Overlap Discrete Wavelet Package Transform) [136]	,
GAN-based Multi-stage PCA [118]	,
Estimating probability density with deep feature embedding [119]	,
t-SNE (t-Distributed Stochastic Neighbour Embedding) [77]	,
+ t-SNE on CNN [120]	,
+ t-SNE, activation atlas on GoogleNet [121]	,
+ t-SNE on latent space in meta-material design [122]	,
+ t-SNE on genetic data [137]	,
+ mm-t-SNE on phenotype grouping [138]	,
Laplacian Eigenmaps visualization for Deep Generative Model [124]	,
KNN (k-nearest neighbour) on multi-center low-rank rep. learning (MCLRR) [125]	,
KNN with triplet loss and <i>query-result activation map pair</i> [139]	,
Group-based Interpretable NN with RW-based Graph Convolutional Layer [123]	,
TCAV (Testing with Concept Activation Vectors) [96]	,
+ RCV (Regression Concept Vectors) uses TCAV with Br score [140]	,
+ Concept Vectors with UBS [141]	,
+ ACE (Automatic Concept-based Explanations) [56] uses TCAV	,
Influence function [129] helps understand adversarial training points	,
Representer theorem [130]	,
SocRat (Structured-output Causal Rationalizer) [127]	,
Meta-predictors [126]	,
Explanation vector [128]	,
# Also listed elsewhere: [14], [43], [85], [94]	N
# Also listed elsewhere: [14], [60], [85] etc	N
CNN with separable model [142]	,
Information theoretic: Information Bottleneck [98], [99]	,
Database of methods v.s. interpretability [10]	N
Case-Based Reasoning [143]	,



Explanations

Some issues

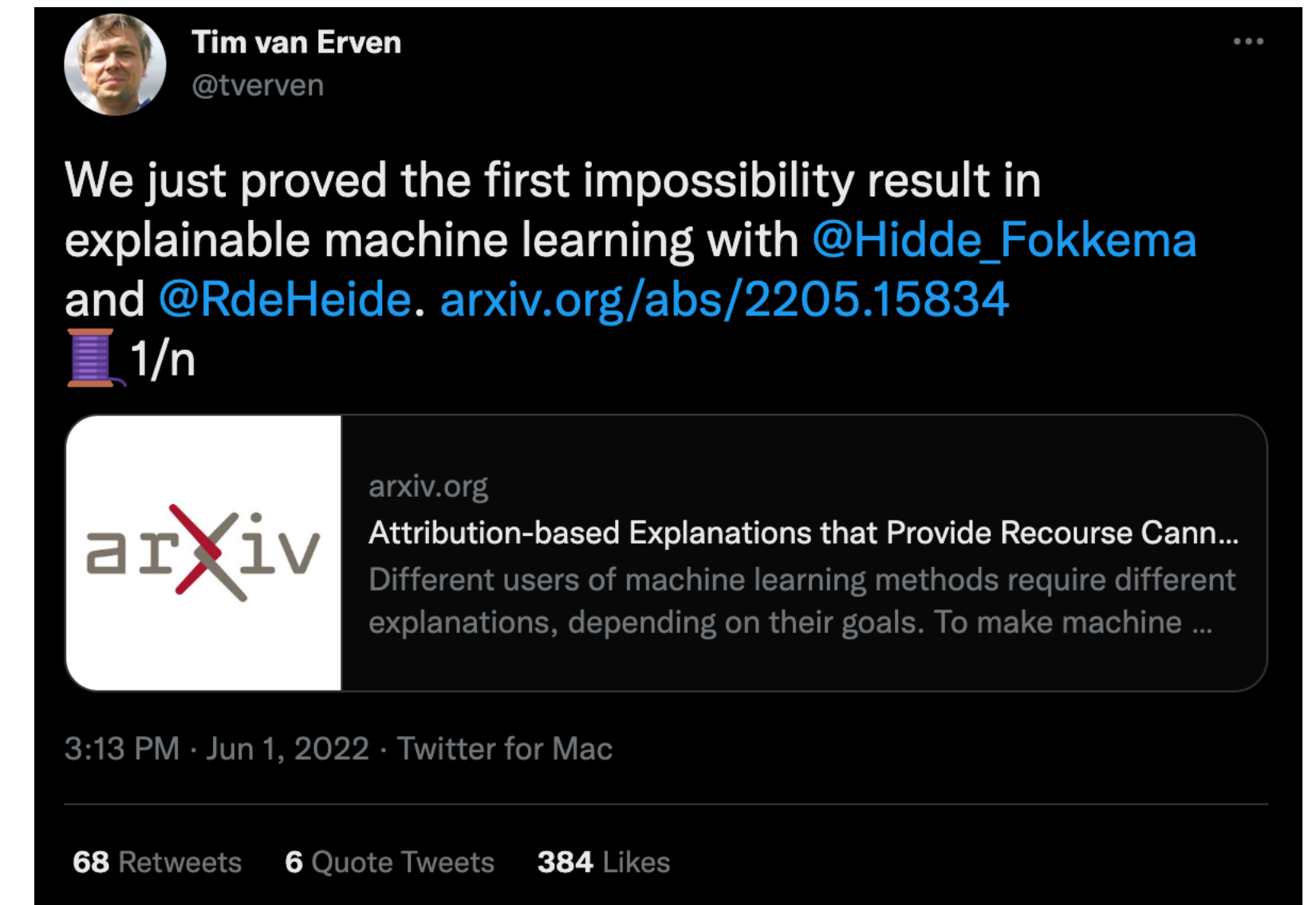
- ▶ Easily manipulated
- ▶ Disagreement problem
- ▶ Can be Unreliable



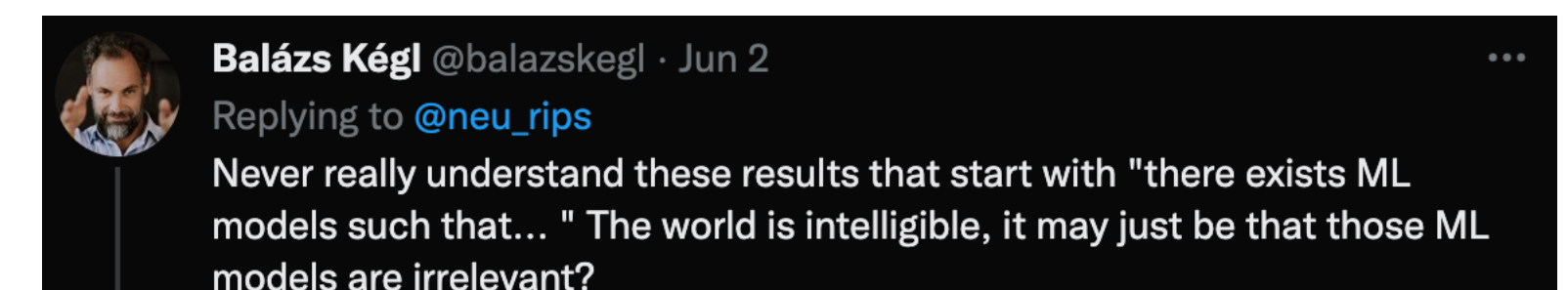
Explanations

Call for Rigor

- ▶ Mythos of model interpretability, [Zachary Lipton, 2017]
- ▶ Towards a rigorous science of interpretable machine learning, [Doshi-Velez, Kim, 2017]
- ▶ “Interpretability research suffers from an over-reliance on intuition-based approaches that risk—and in some cases have caused—illusory progress and misleading conclusions”, [Leavitt, Morcos, 2020]



Some people liked this

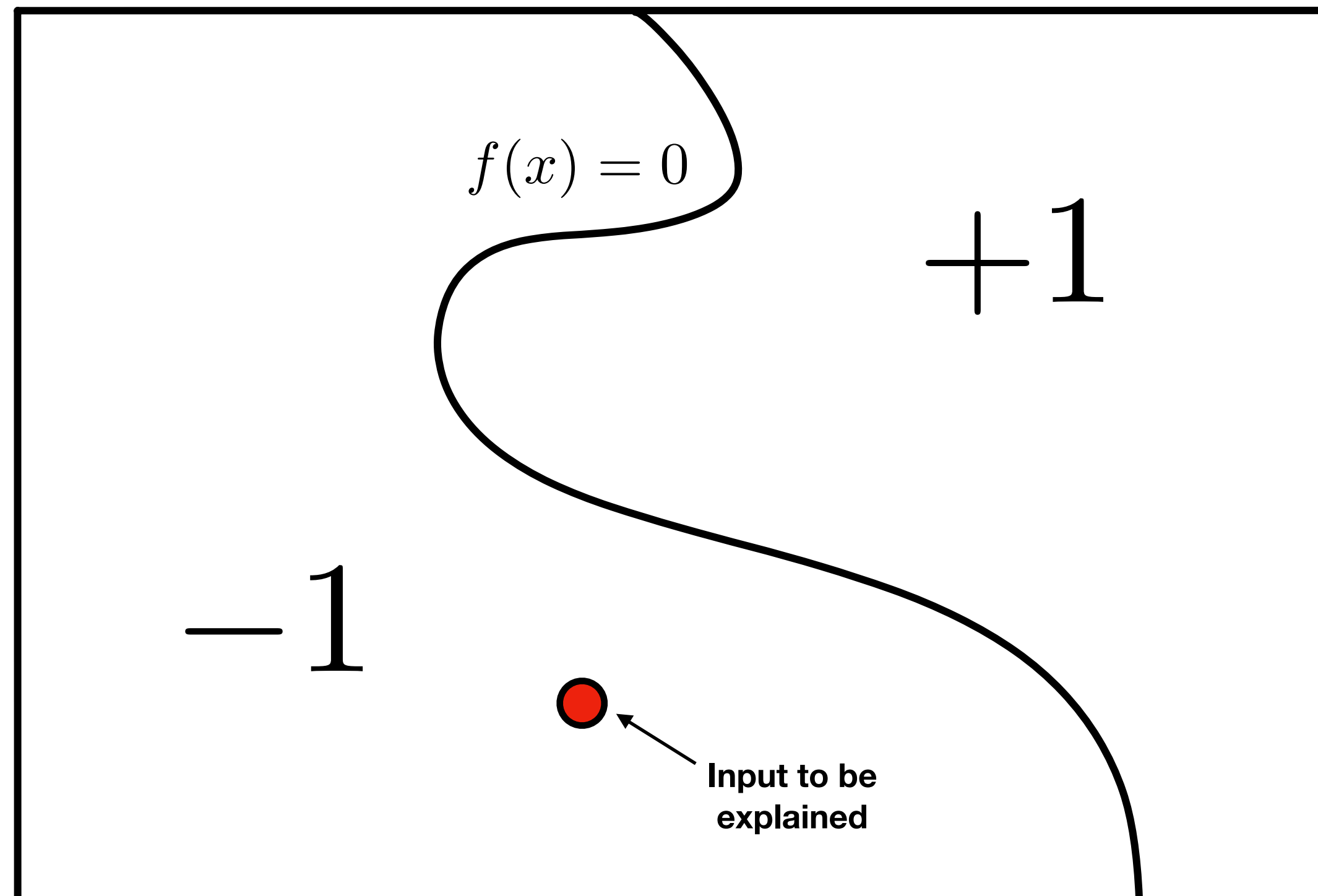


Some people didn't

Attribution methods

Setting

Post-Hoc and local explanations



Machine learning model, e.g. a classifier:

$$f: \mathcal{X} \subseteq \mathbb{R}^d \rightarrow [0, 1], \begin{bmatrix} x_1 \\ \vdots \\ x_d \end{bmatrix} \mapsto y$$

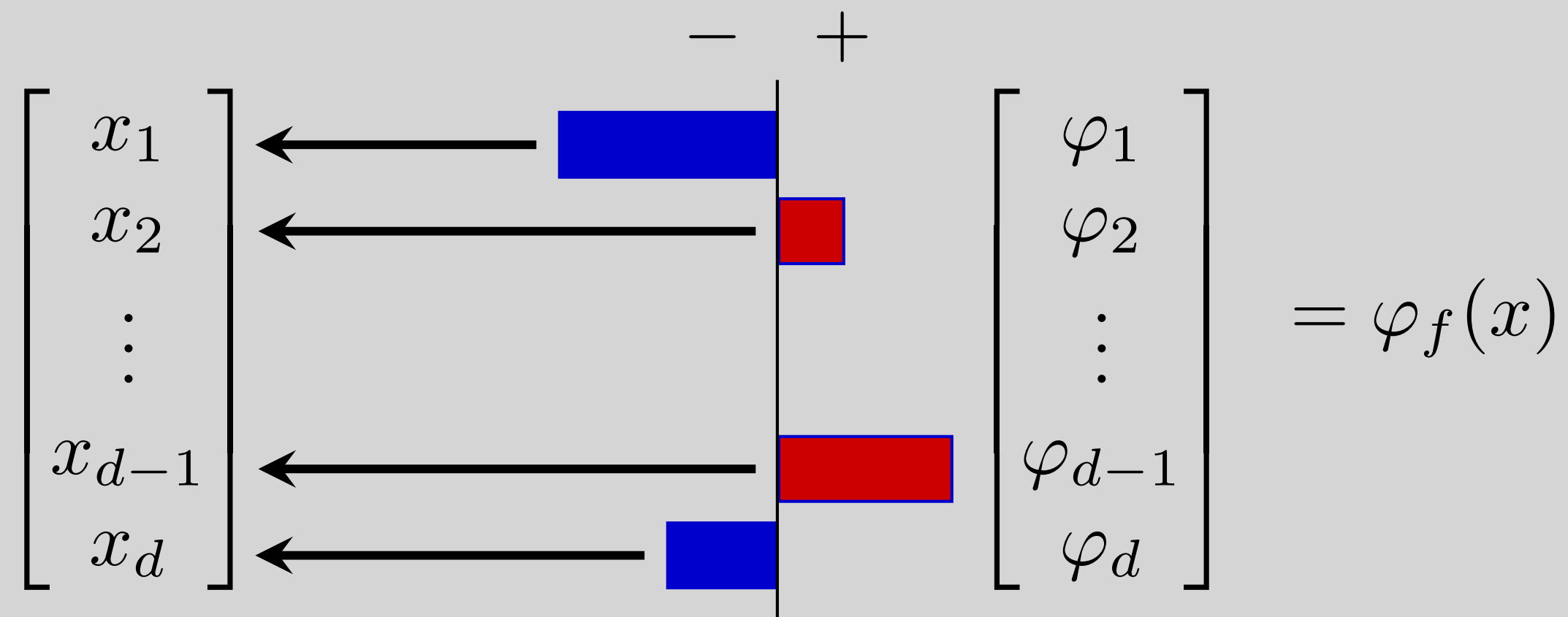
- **Local:** Only explain the part of f that is relevant for x
- **Post-Hoc:** The function f is given and fixed

Setting

Attribution methods

Machine learning model, e.g. a classifier:

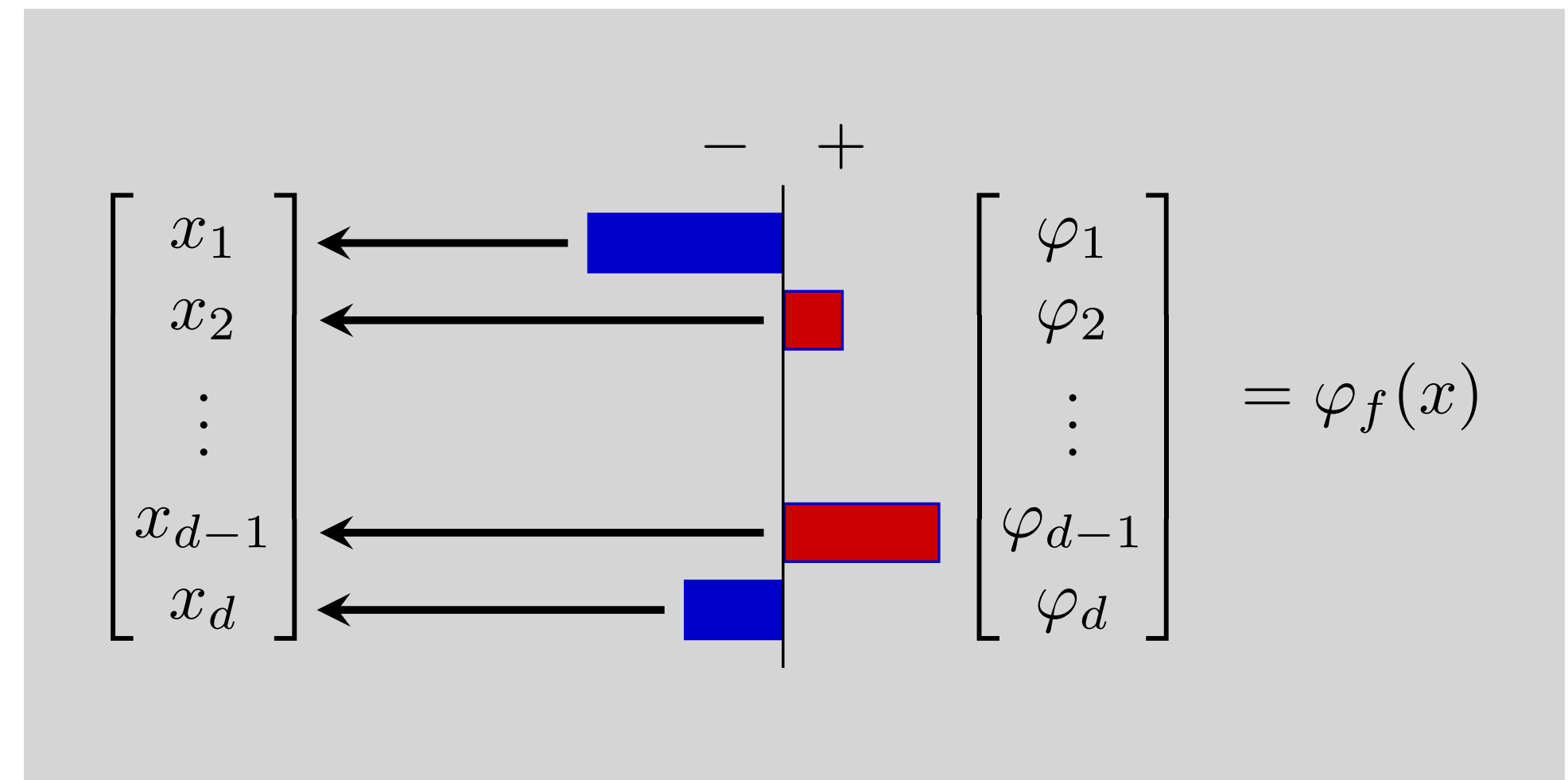
$$f: \mathcal{X} \subseteq \mathbb{R}^d \rightarrow [0, 1], \begin{bmatrix} x_1 \\ \vdots \\ x_d \end{bmatrix} \mapsto y$$



$\varphi_f(x) \in \mathbb{R}^d$ attributes **a weight to each feature** which explains **how important** the feature was for the **classification of x of f**

Example

Attribution methods



f linear, low dimension d

$$f(x) = \theta_0 + \sum_{i=1}^d x_i \theta_i$$

$$\varphi_f(x)_i = \theta_i$$

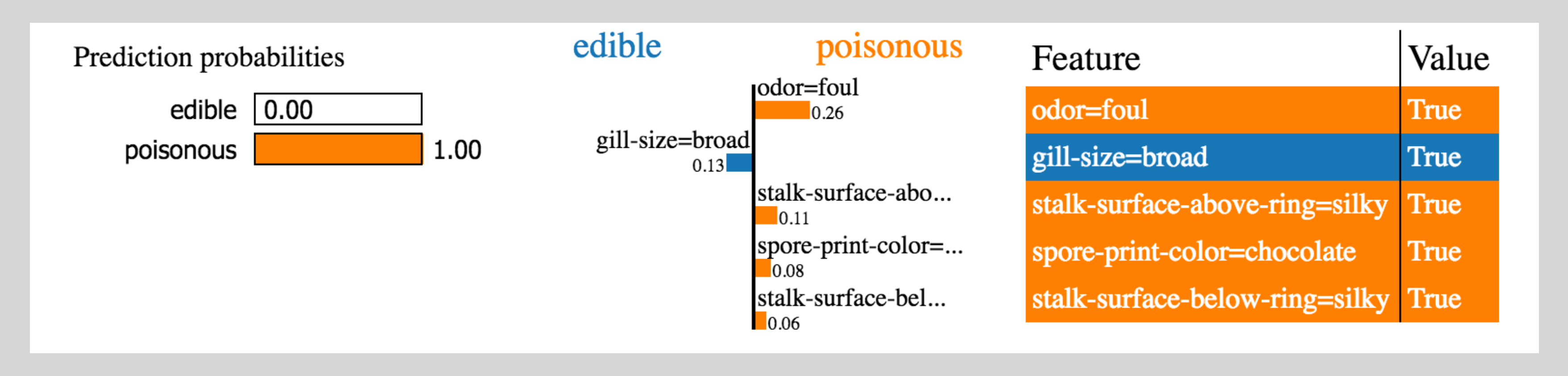
- ▶ In general φ_f will depend on x
- ▶ Most methods follow this example, by locally linearising around x

Examples (LIME)

Lime: Extract local linear approximations of f near x and report coefficients

- Optionally: Apply some dimension reduction before linearising.

Lime for tabular data¹



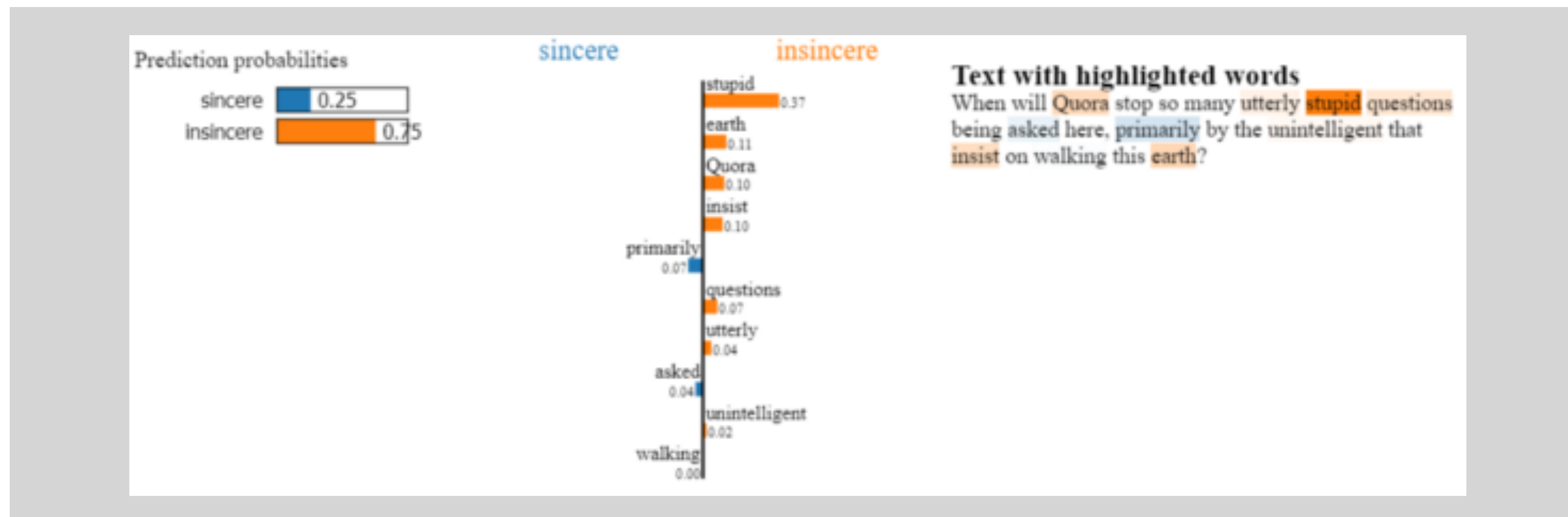
¹Image source: <https://github.com/marcoctr/lime>

Examples (LIME for Text)

Lime: Extract local linear approximations of f near x and report coefficients

- Optionally: Apply some dimension reduction before linearising.

Lime for text data²



²Image source: <https://towardsdatascience.com/what-makes-your-question-insincere-in-quora-26ee7658b010>.

Examples (LIME for Images)

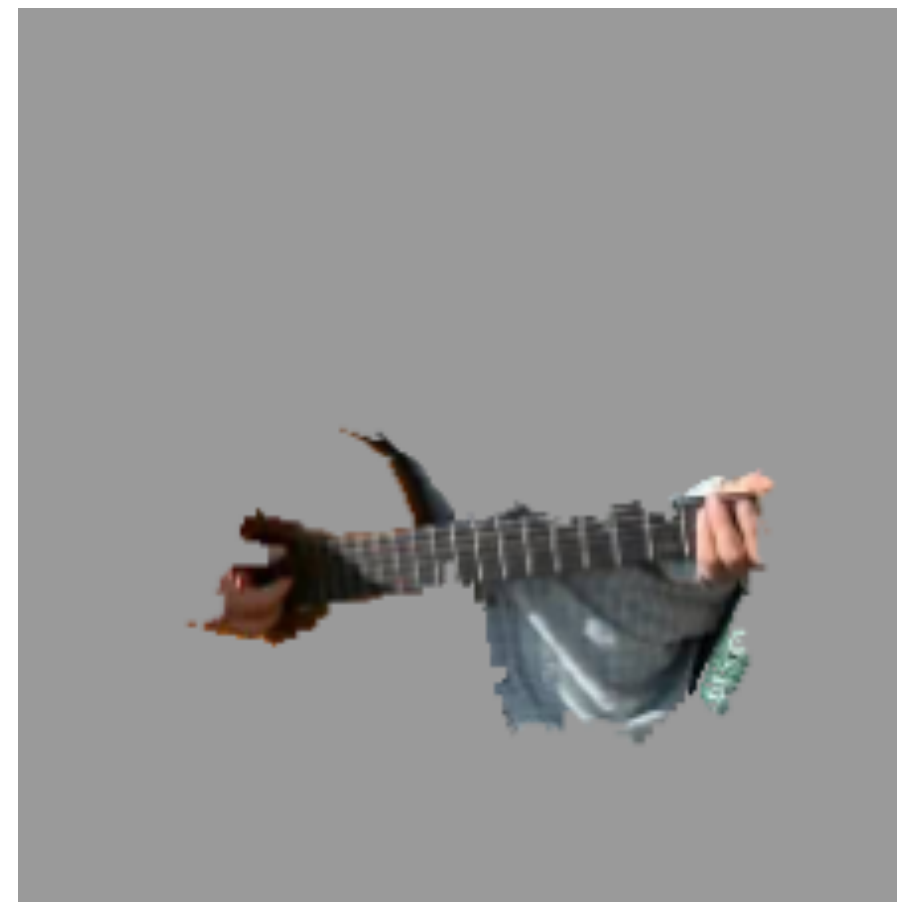
Lime: Extract local linear approximations of f near x and report coefficients

- Optionally: Apply some dimension reduction before linearising.

Lime for image data³



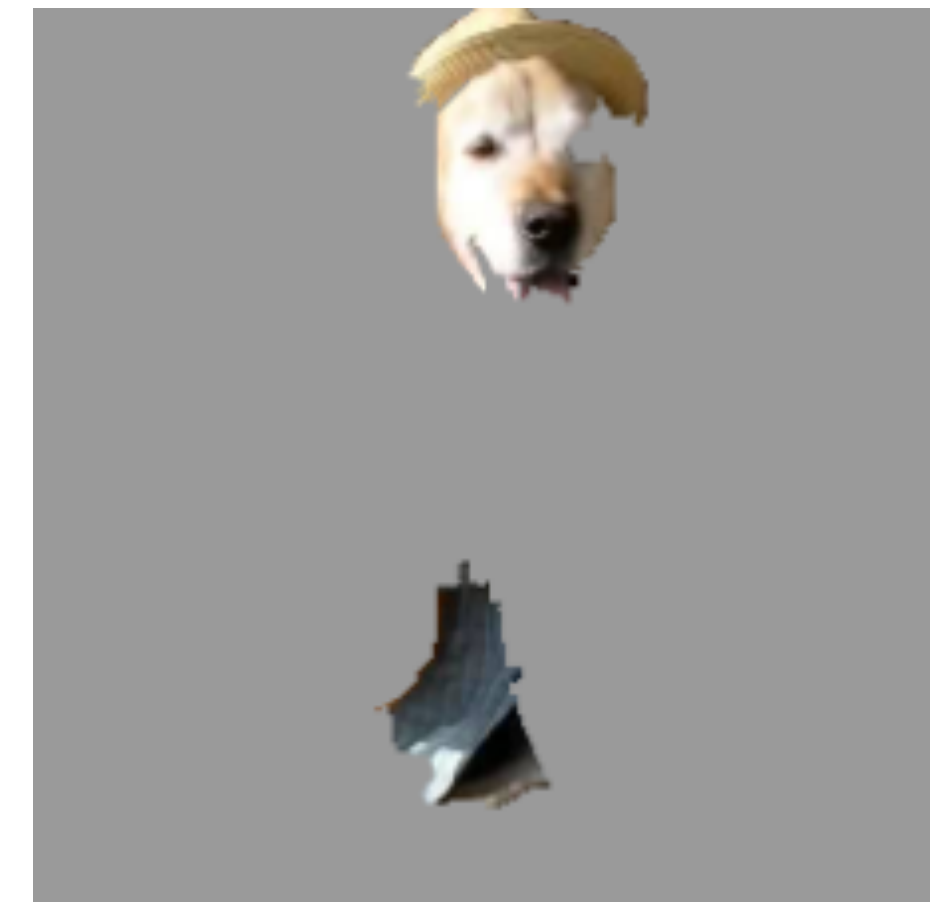
(a) Original Image



(b) Explaining *Electric guitar*



(c) Explaining *Acoustic guitar*



(d) Explaining *Labrador*

³Image source: [Ribeiro et al., 2016]

Examples (Gradient)

Gradient methods

- ▶ Vanilla gradient:

$$\varphi_f(x) = \nabla f(x)$$

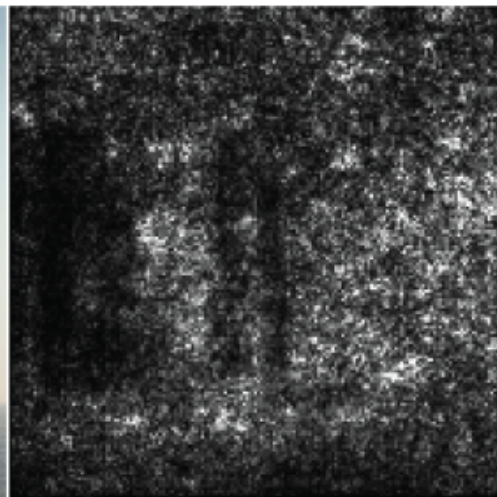
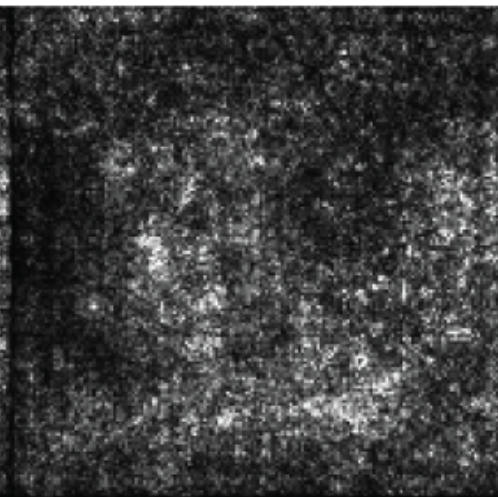
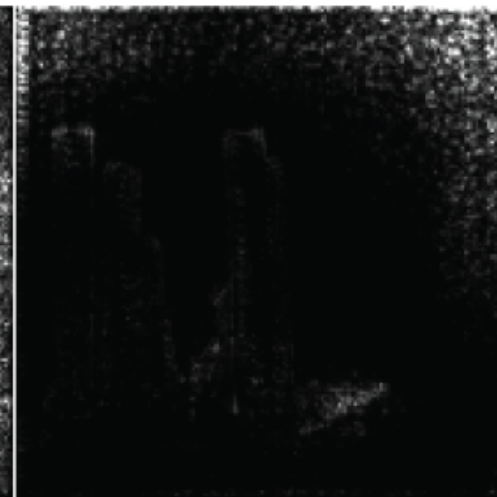
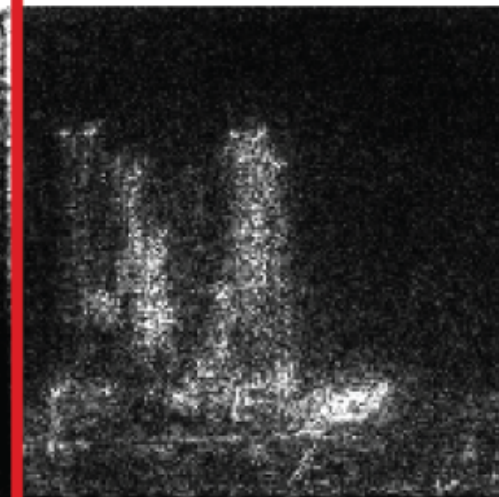
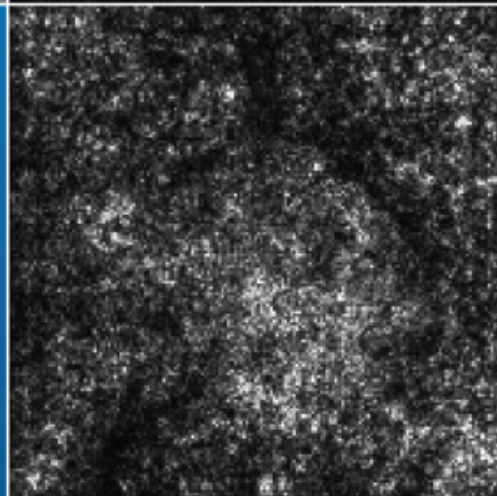
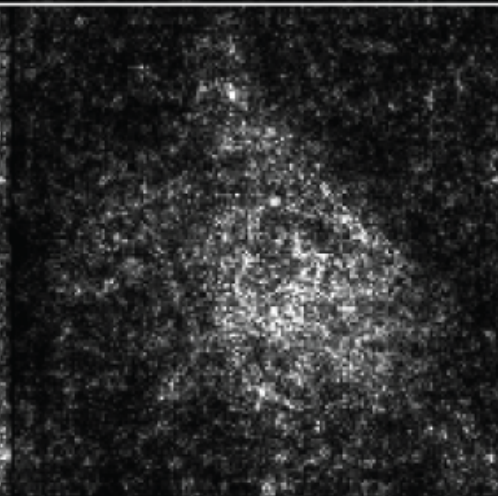
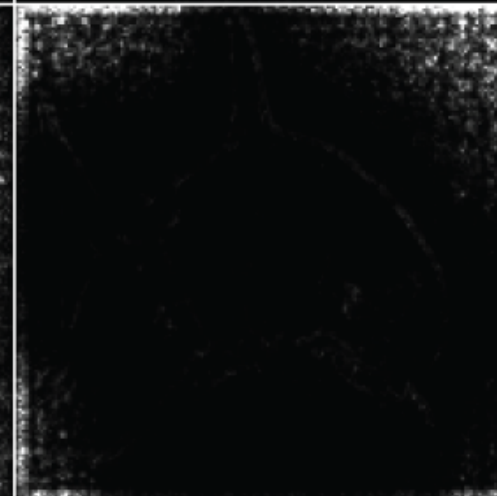
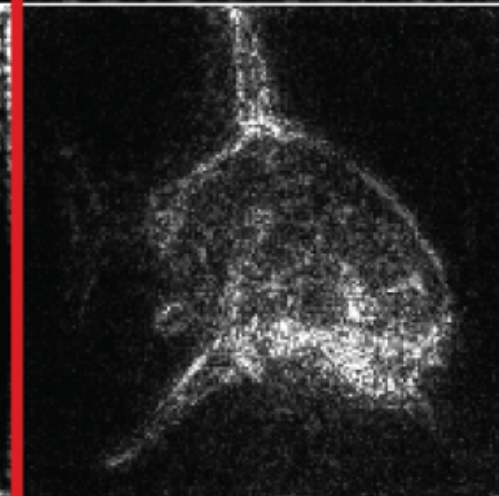
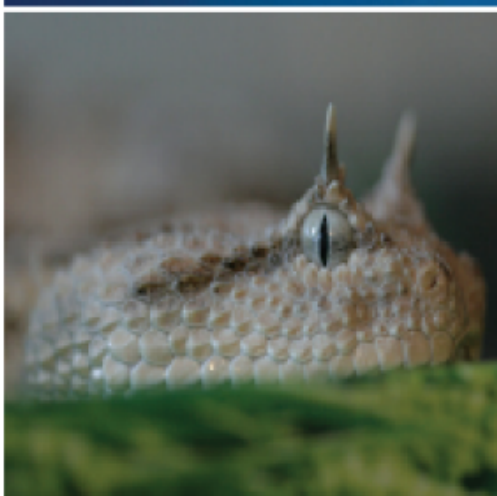
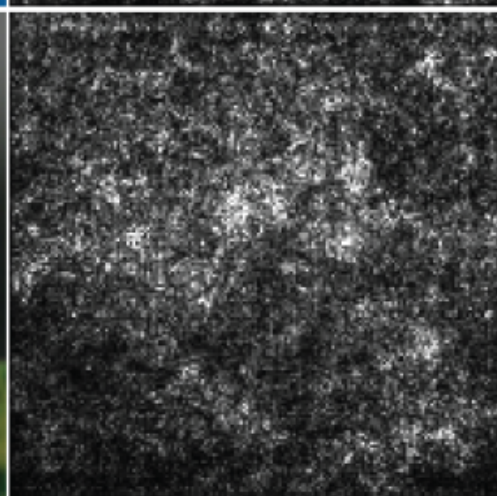
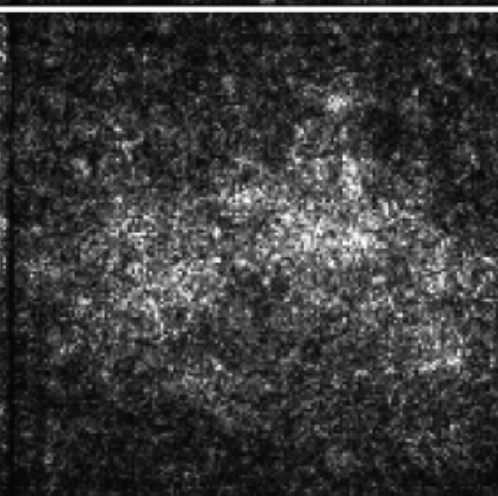
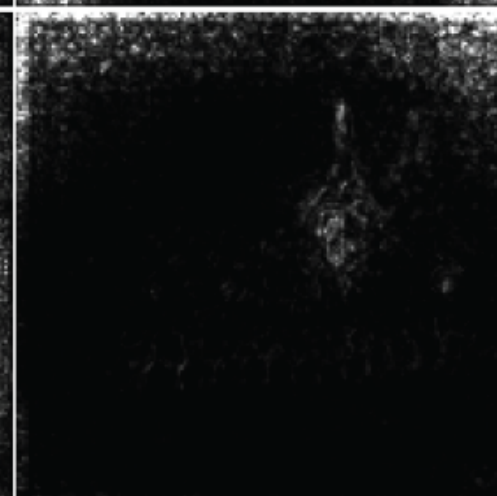
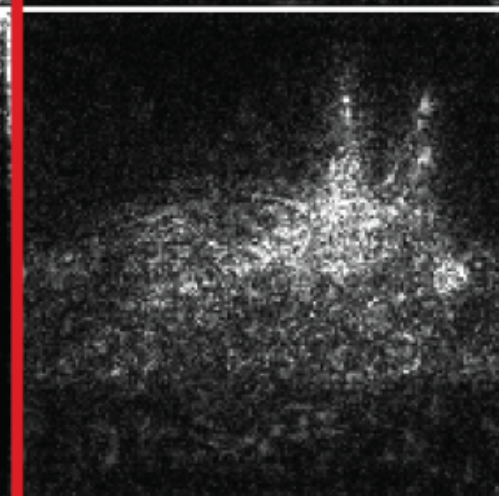
- ▶ SmoothGrad:

$$\varphi_f(x) = \mathbb{E}_{Z \sim \mathcal{N}(x, \Sigma)} [\nabla f(Z)]$$

- ▶ Integrated Gradients:

$$\varphi_f(x) = (x - x_0) \int_0^1 \nabla f(x_0 + t(x - x_0)) dt$$

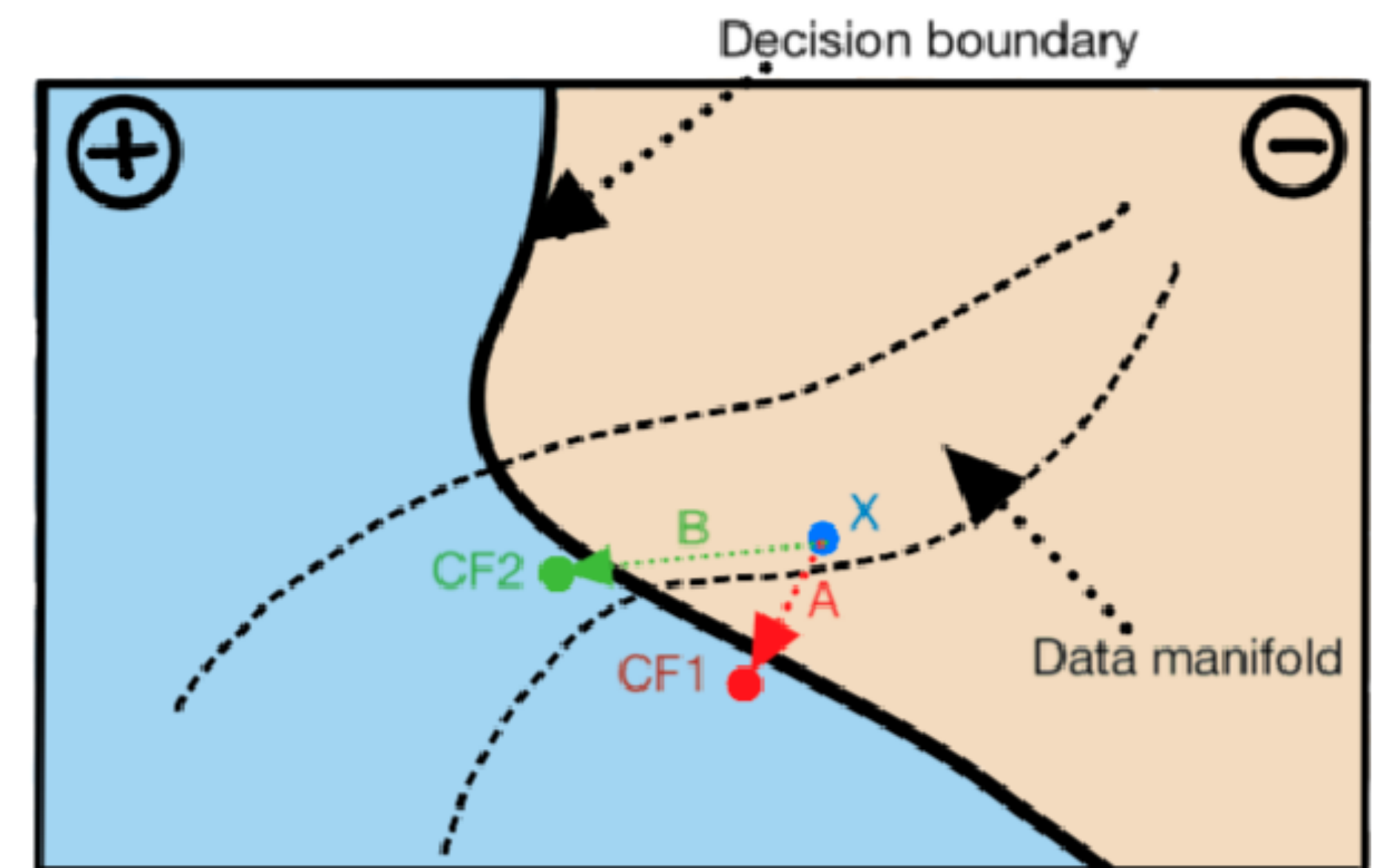
- ▶ ...

Gradient					
	Vanilla	Integrated	Guided BackProp	SmoothGrad	
drilling platform					
great white shark					
hognose snake					

Counterfactuals

Example

"If your Income would have been € 40.000,- instead of € 35.000,-, your loan application would have been accepted"



⁵Image source: [Verma et al., 2020]

Counterfactuals as attributions

Definition

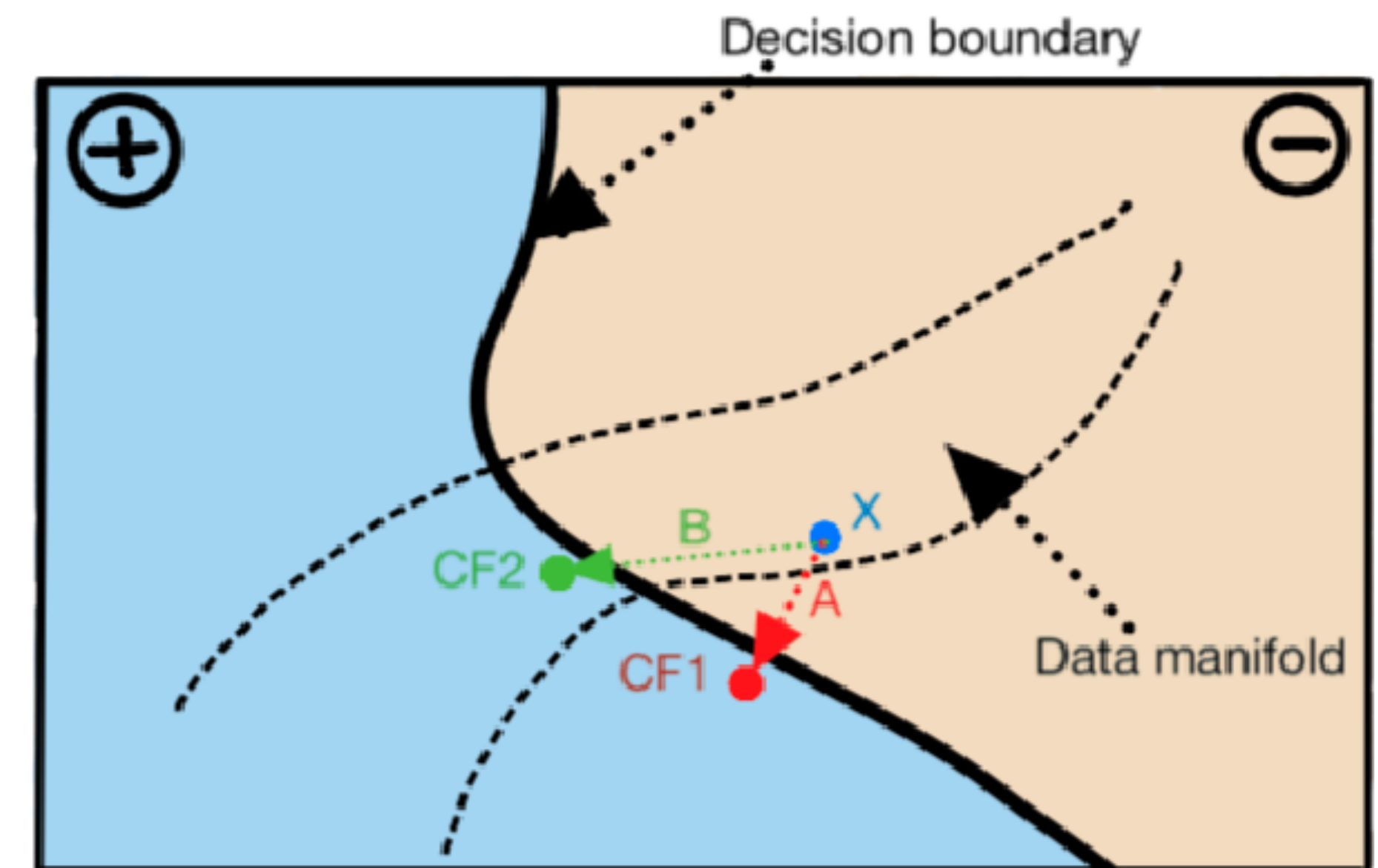
Consider Binary classification $f: \mathcal{X} \rightarrow \{-1, 1\}$
and
let $x \in \mathcal{X}$.

A *counterfactual* x^{CF} for x is

$$x^{\text{CF}} \in \arg \min_{y \in \mathcal{C}} \|x - y\| \quad \text{s.t.} \quad f(x^{\text{CF}}) \neq f(x)$$

Counterfactuals can be seen as Attributions.
Write

$$\varphi_f(x) = x^{\text{cf}} - x$$



What are Good Explanations/Attributions?

- ▶ How to say some explanations are **better than others**?
- ▶ What is the **(implicit) goal** of the explanations?

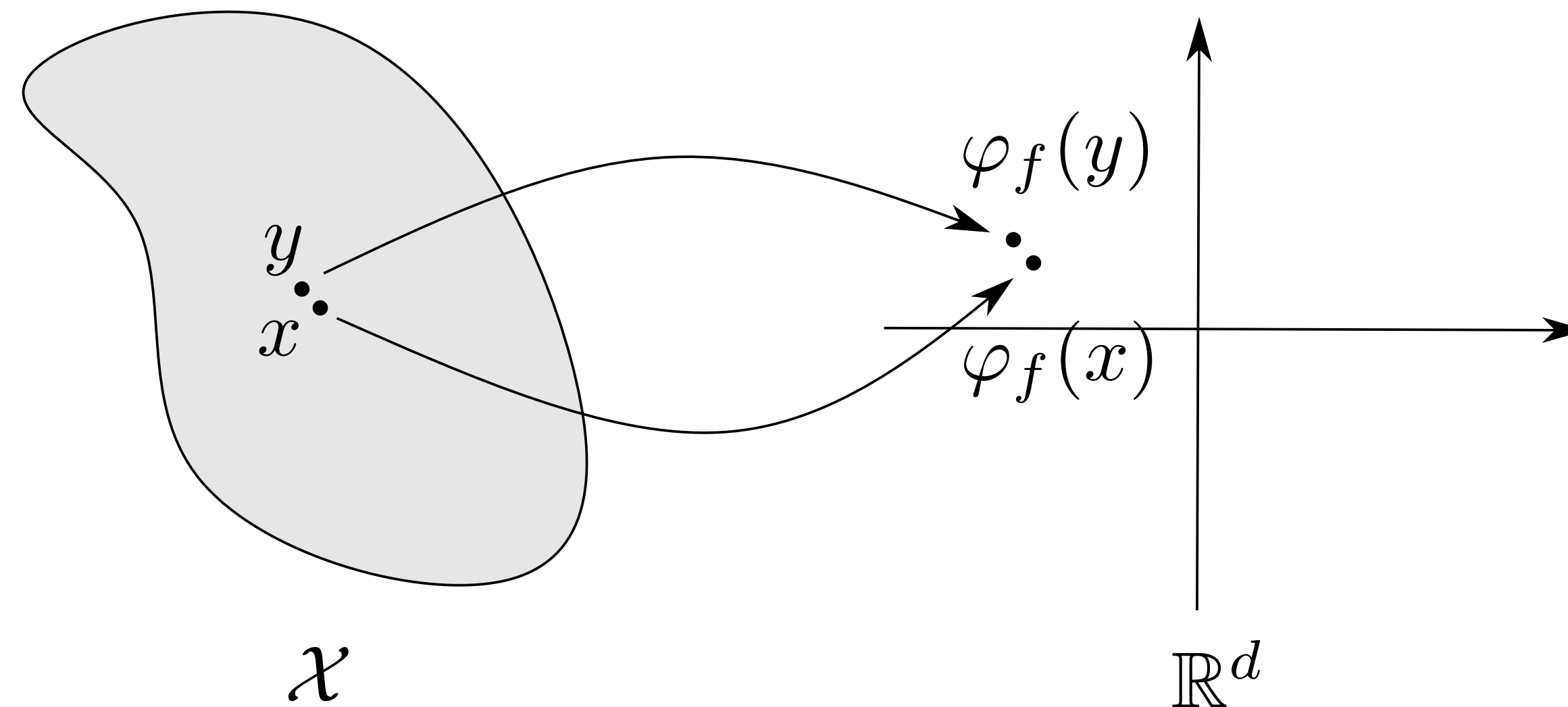
Robustness & Recourse sensitivity

Robustness

Definition

An attribution method φ_f for f is called **Robust** if it is continuous

Similar users require similar explanations



Recourse sensitivity

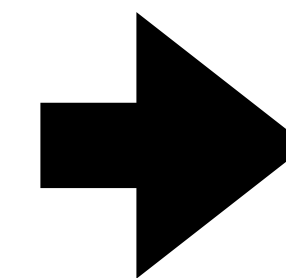
Motivation

User has some goal in mind:

- ▶ Wants to get a loan
- ▶ Increase their credit score
- ▶ Increase a probability
- ▶ Wants to upload a profile picture to get an OV card.

The explanation should allow the user to reach this goal

REJECTED



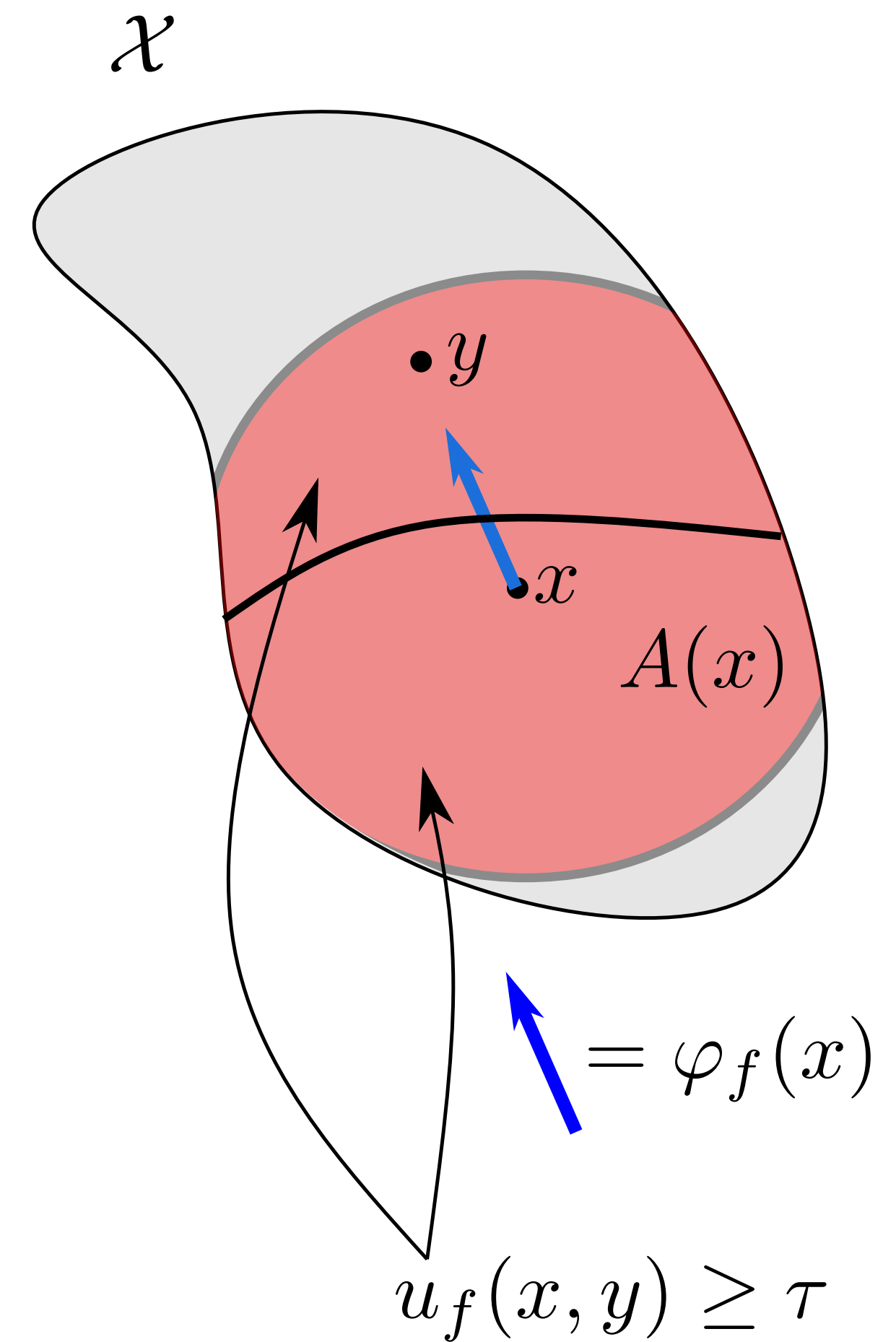
ACCEPT

Recourse sensitivity

Informal definition

An Attribution method is called ***Recourse Sensitive*** if the user can achieve a sufficient utility increase when moving in the direction of $\varphi_f(x)$

This is very weak form of Recourse!



Recourse sensitivity

Utility & Attainable points

Measure if some utility $u_f: \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$ exceeds some threshold $u_f(x, y) \geq \tau$:

- ▶ Undesirable classification: $u_f(x, y) = f(y) \geq 0$
- ▶ Increase score: $u_f(x, y) = f(y) - f(x) \geq \tau$
- ▶ Decrease a probability: $u_f(x, y) = \frac{f(x)}{f(y)} \geq \frac{1}{1-p} = \tau$

Define set of attainable points from x

$$A(x) = \{y \in \mathcal{X} \mid \|x - y\| \leq \delta, y \in C(x)\}$$

The set $C(x)$ will impose some constraints. Examples:

- ▶ $C(x) = \mathcal{X}$, Unrestricted case,
- ▶ $C(x) = \{y \in \mathcal{X} \mid \|x - u\|_0 \leq k\}$, Sparse change,
- ▶ $C(x) = \{u \in \mathcal{X} \mid y = x + \alpha z, \alpha \geq 0, z \in D\}$, Certain Directions D .

Recourse sensitivity

Definition

Definition

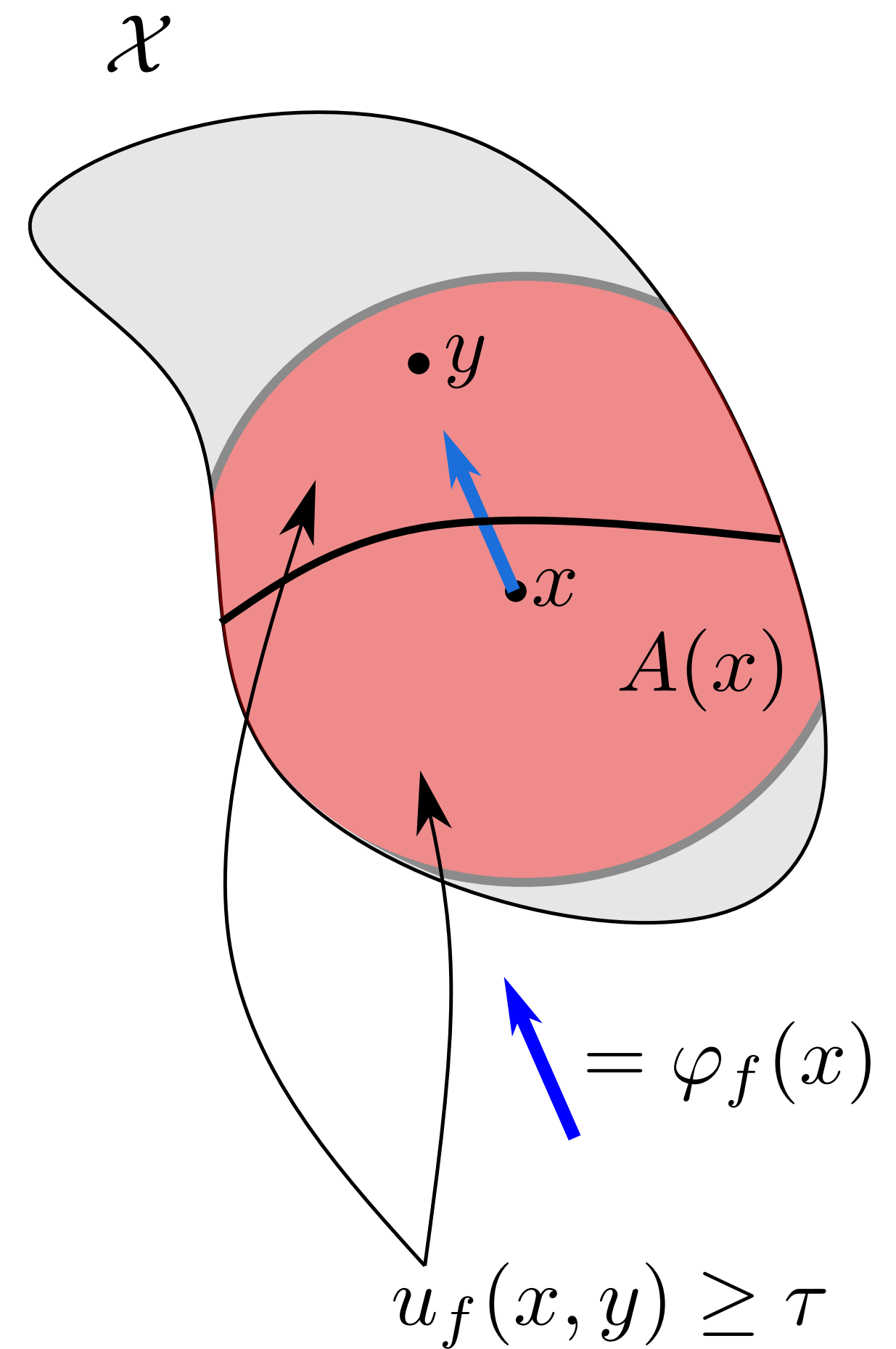
Consider the points close to x that achieve sufficient utility

$$U(x) = \{y \in \mathcal{X} \mid u_f(x, y) \geq \tau, \|x - y\| \leq \delta\}$$

An Attribution function φ_f is called **Recourse Sensitive** if

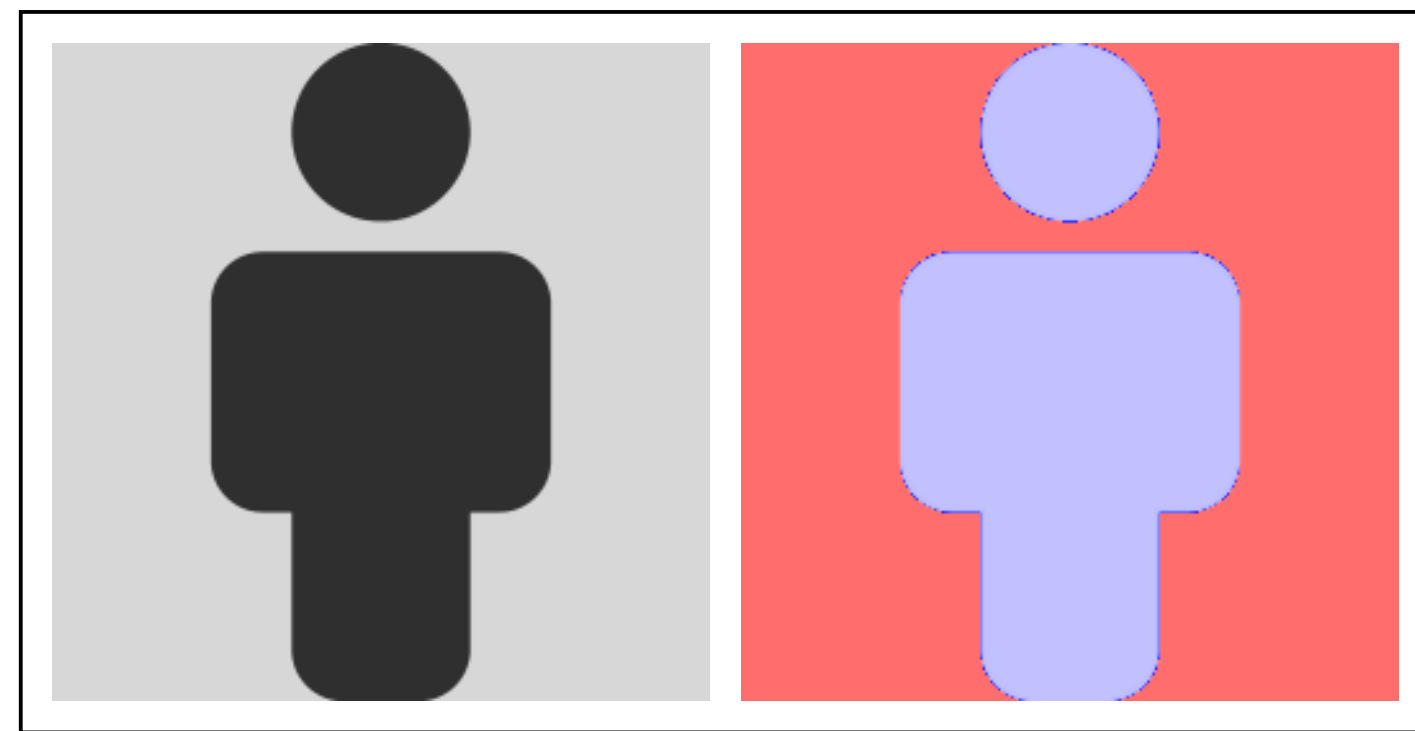
$$\varphi_f(x) = \alpha(y - x), \quad \alpha > 0 \text{ and } y \in U(x),$$

for all $x \in \mathcal{X}$ for which $U(x) = \emptyset$.

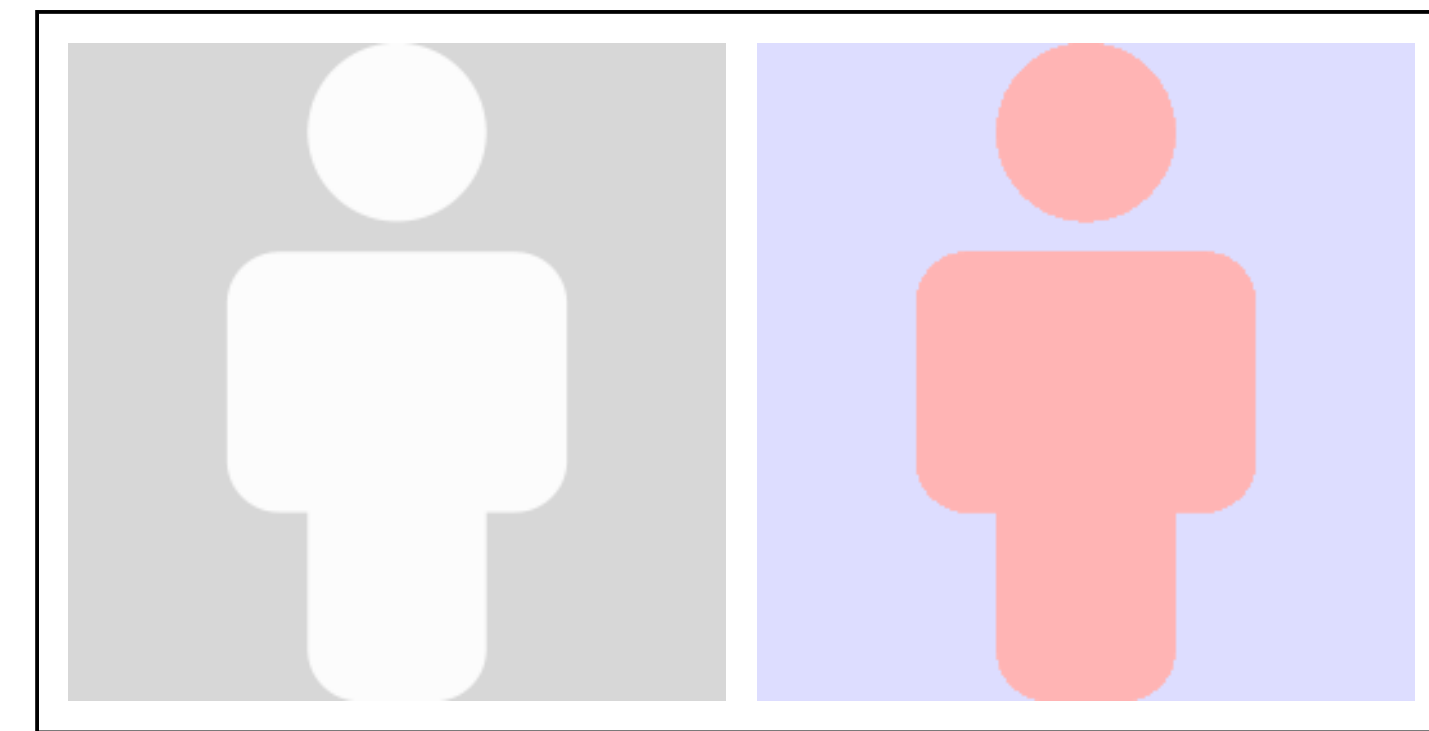


Recourse sensitivity

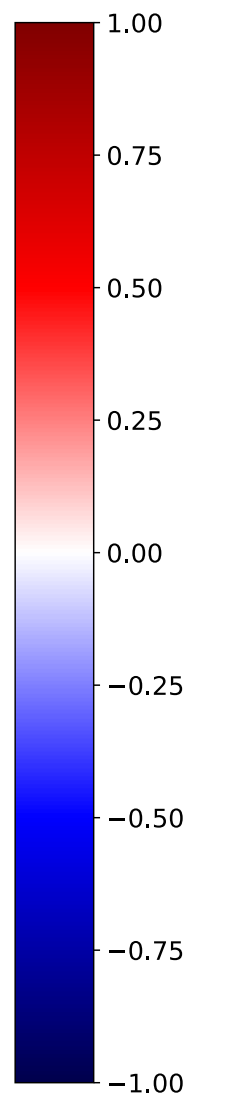
Example



(a) Accepted profile picture



(b) Rejected profile picture



Impossibility

Impossibility result

Attribution methods cannot always

- Provide Recourse
- Be Robust

Impossibility result

Specific case (Binary classification)

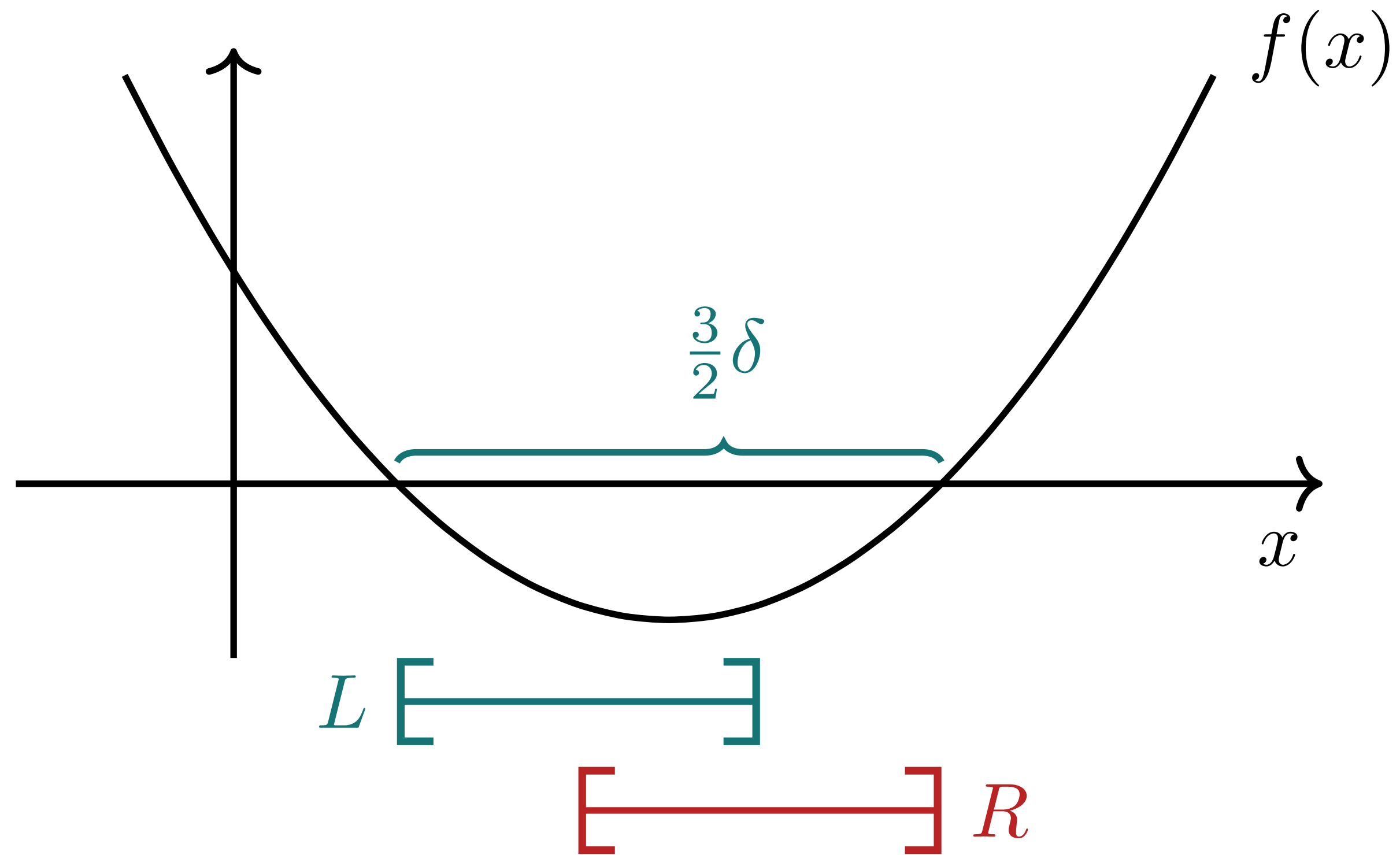
Setting

- $\mathcal{X} = \mathbb{R}^d$,
- $u_f(x, y) = f(y)$,
- $\tau = 0, \delta > 0$.

Theorem

There exists a continuous function f such that no attribution method φ_f can be both recourse sensitive and continuous

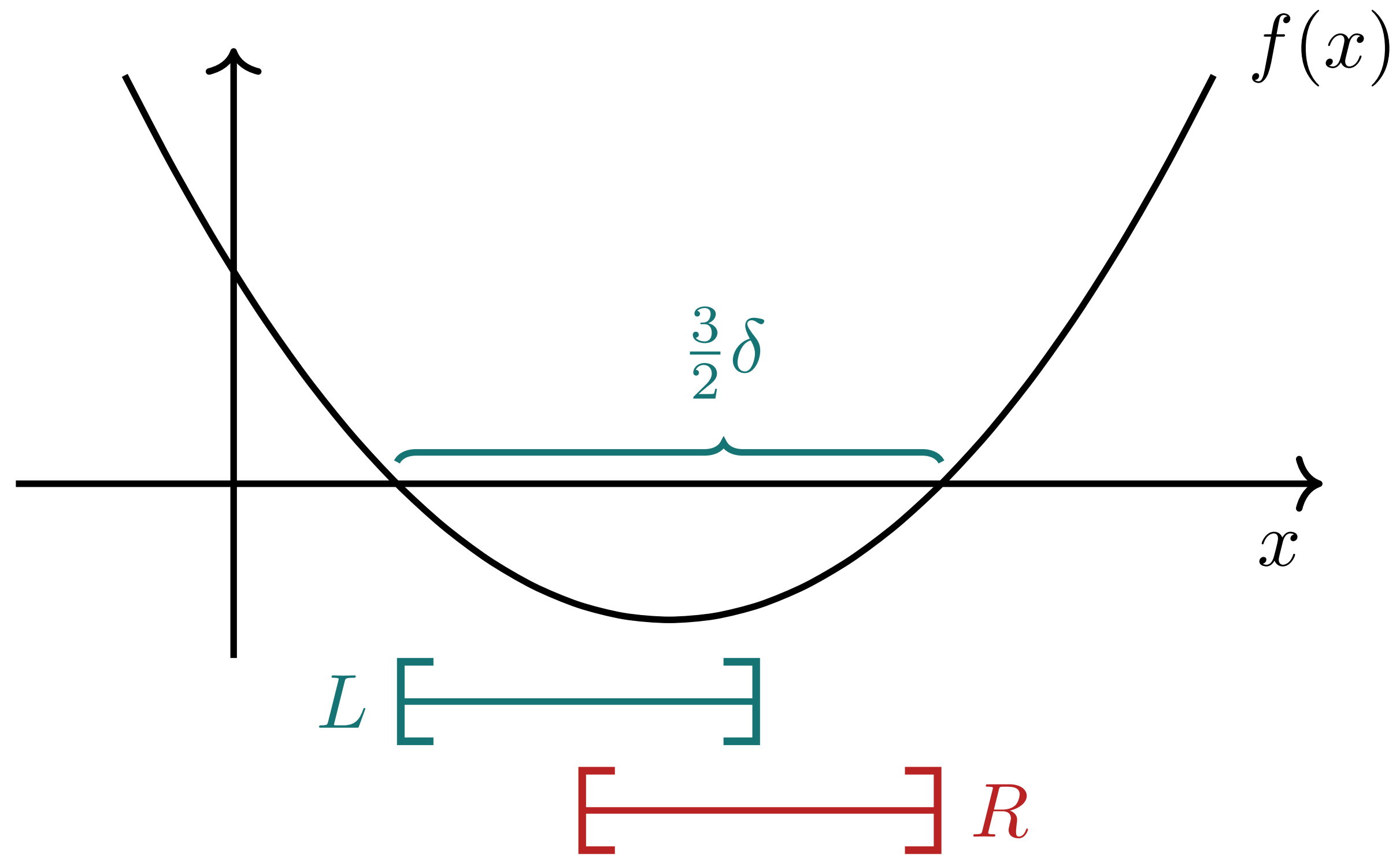
Proof sketch



$R = \{x \mid \text{recourse is possible by moving at most } \delta \text{ left}\}$

$L = \{x \mid \text{recourse is possible by moving at most } \delta \text{ left}\}$

Proof sketch

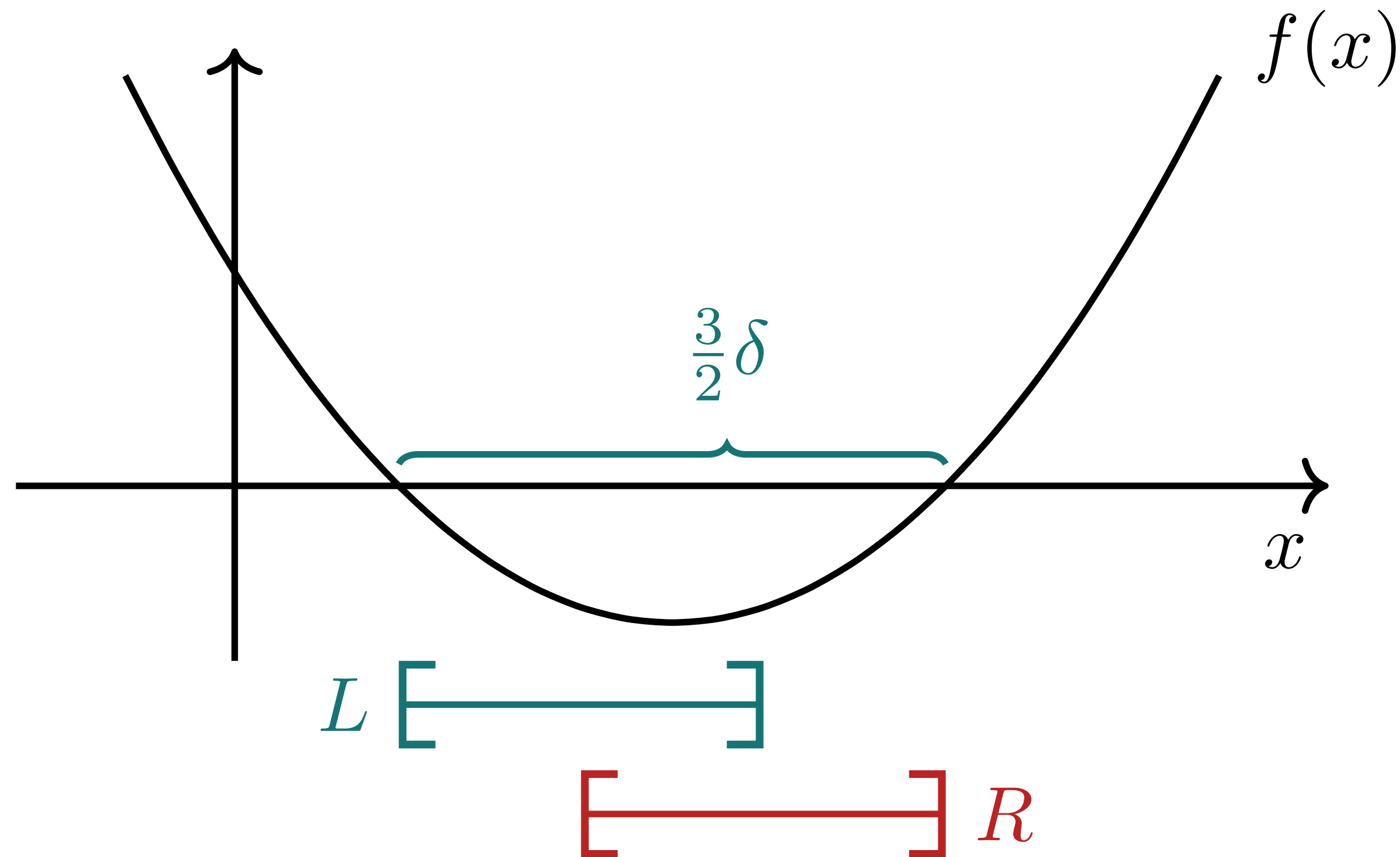


$R = \{x \mid \text{recourse is possible by moving at most } \delta \text{ left}\}$

$L = \{x \mid \text{recourse is possible by moving at most } \delta \text{ left}\}$

$$\varphi_f(x) = \begin{cases} < 0 & \text{for } x \in L \setminus R \\ > 0 & \text{for } x \in R \setminus L \\ \neq 0 & \text{for } x \in L \cap R \end{cases}$$

Proof sketch



$R = \{x \mid \text{recourse is possible by moving at most } \delta \text{ left}\}$

$L = \{x \mid \text{recourse is possible by moving at most } \delta \text{ left}\}$

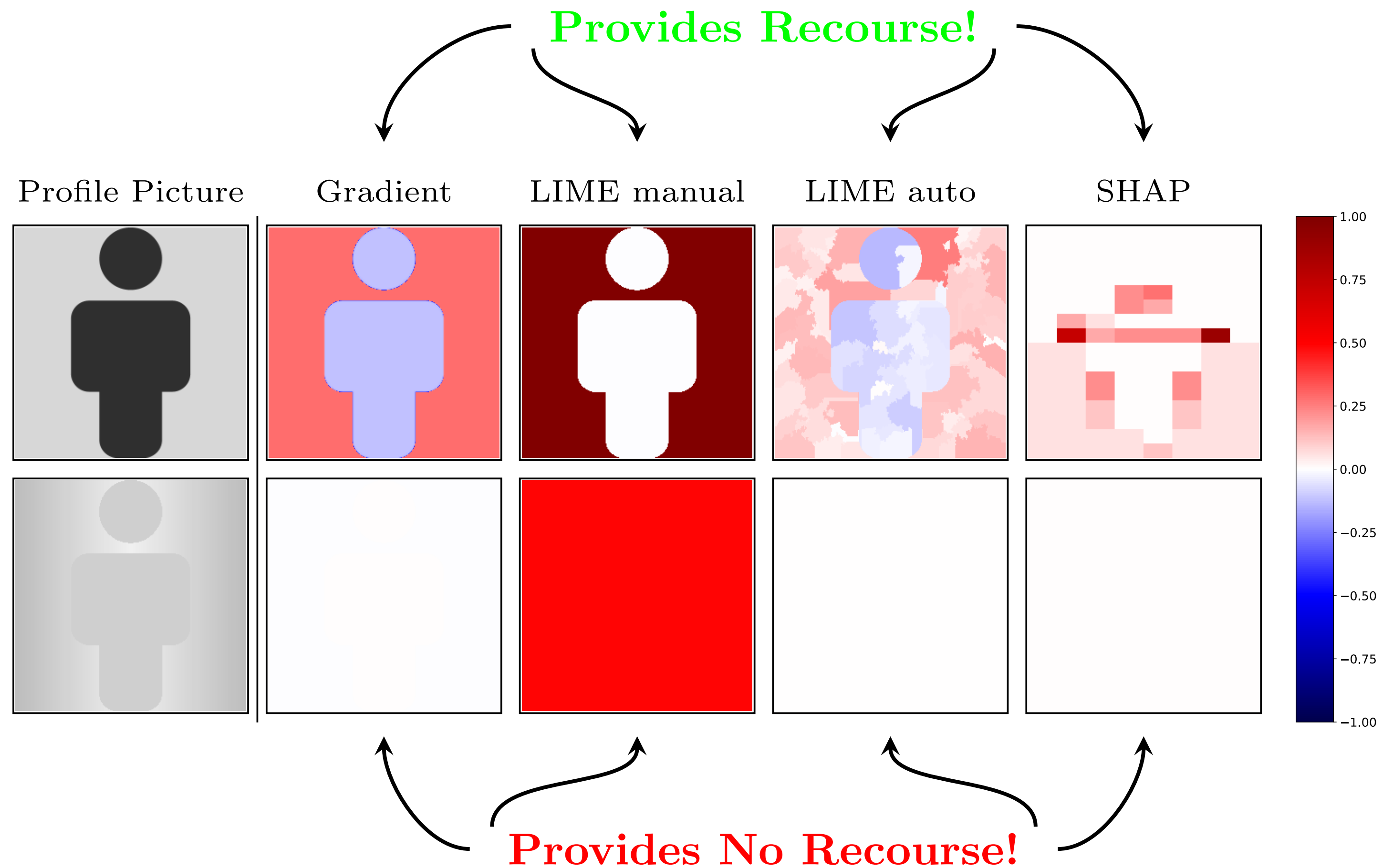
$$\varphi_f(x) = \begin{cases} < 0 & \text{for } x \in L \setminus R \\ > 0 & \text{for } x \in R \setminus L \\ \neq 0 & \text{for } x \in L \cap R \end{cases}$$

But this **contradicts continuity!**
(By the intermediate-value theorem)

This example can be embedded into higher dimensions

Recourse sensitivity

Example



Impossibility result

General case

Theorem

If u_f is of the form $u_f(x, y) = \tilde{u}(f(x), f(y))$ and if there exist $z_1, z_2 \in \mathbb{R}^d$ such that $\tilde{u}(z_1, z_2) \geq \tau$ and $\tilde{u}(z_1, z_1) < \tau$.

Then, there exists a continuous $f: \mathcal{X} \rightarrow \mathbb{R}$ for which no attribution method φ_f can be both recourse sensitive and robust.

Attribution methods cannot always

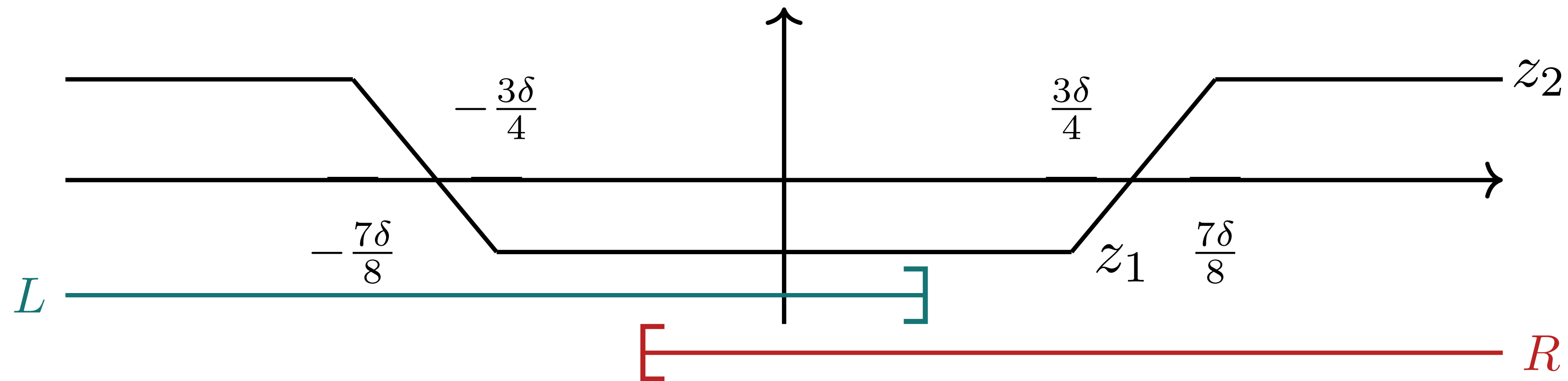
- Provide recourse
- Be continuous

Impossibility result

Proof sketch

Define

- Take z_1, z_2 such that $\tilde{u}(z_1, z_2) \geq \tau$.
- $L = \{x \in \mathcal{X} \mid \text{there exists some } y \in [x - \delta, x] \text{ with } u_f(x, y) \geq \tau\}$,
- $R = \{x \in \mathcal{X} \mid \text{there exists some } y \in [x + \delta, x] \text{ with } u_f(x, y) \geq \tau\}$.

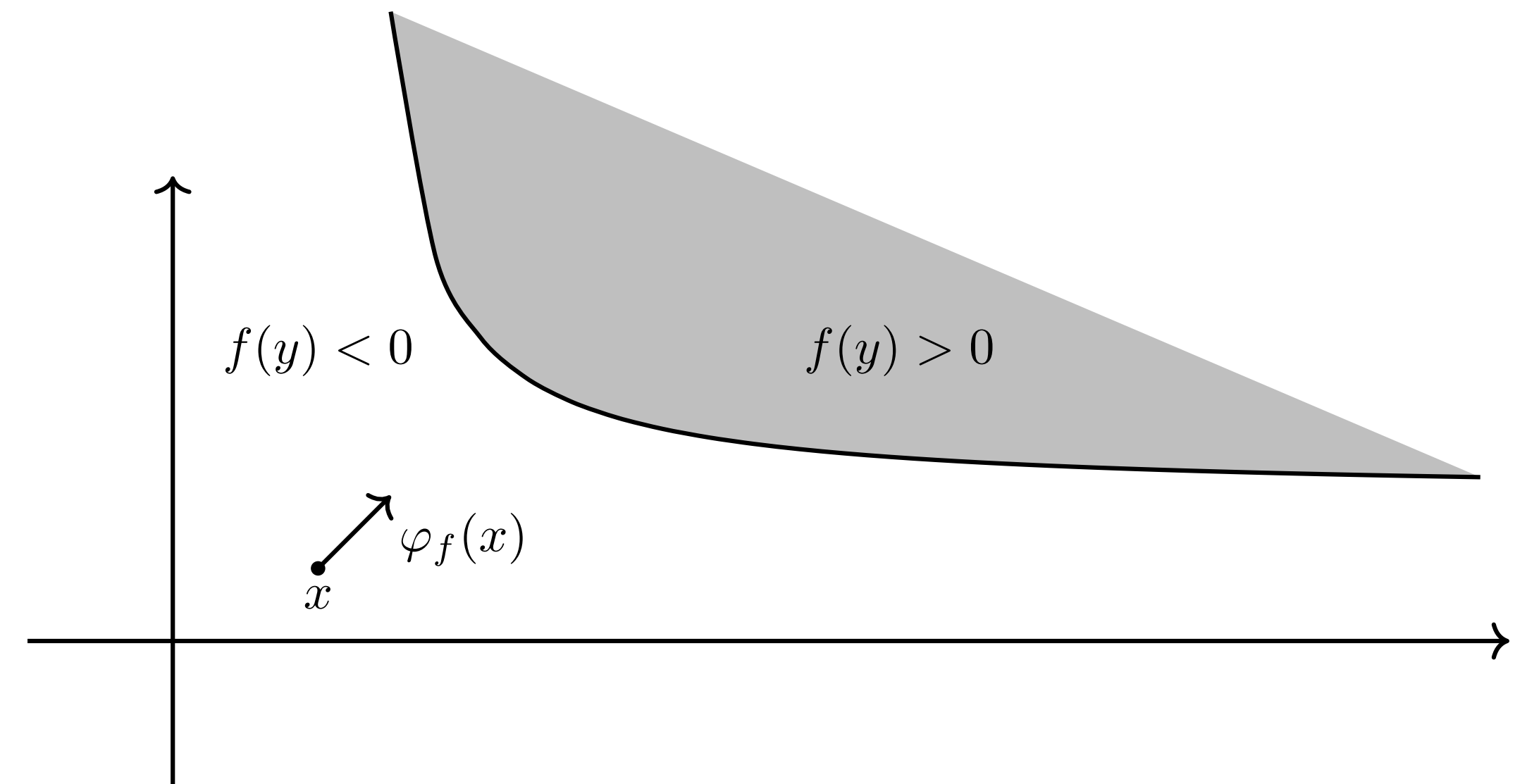


**When is Recourse and
Robustness possible?**

Recourse and Robustness is possible sometimes

Binary classification

- ▶ Preferred class ($u_f(x, y) = f(y) \geq 0$)
- ▶ Let $U = \{x \in \mathcal{X} \mid f(x) > 0\}$ be convex
- ▶ Then Recourse and Robustness is possible!

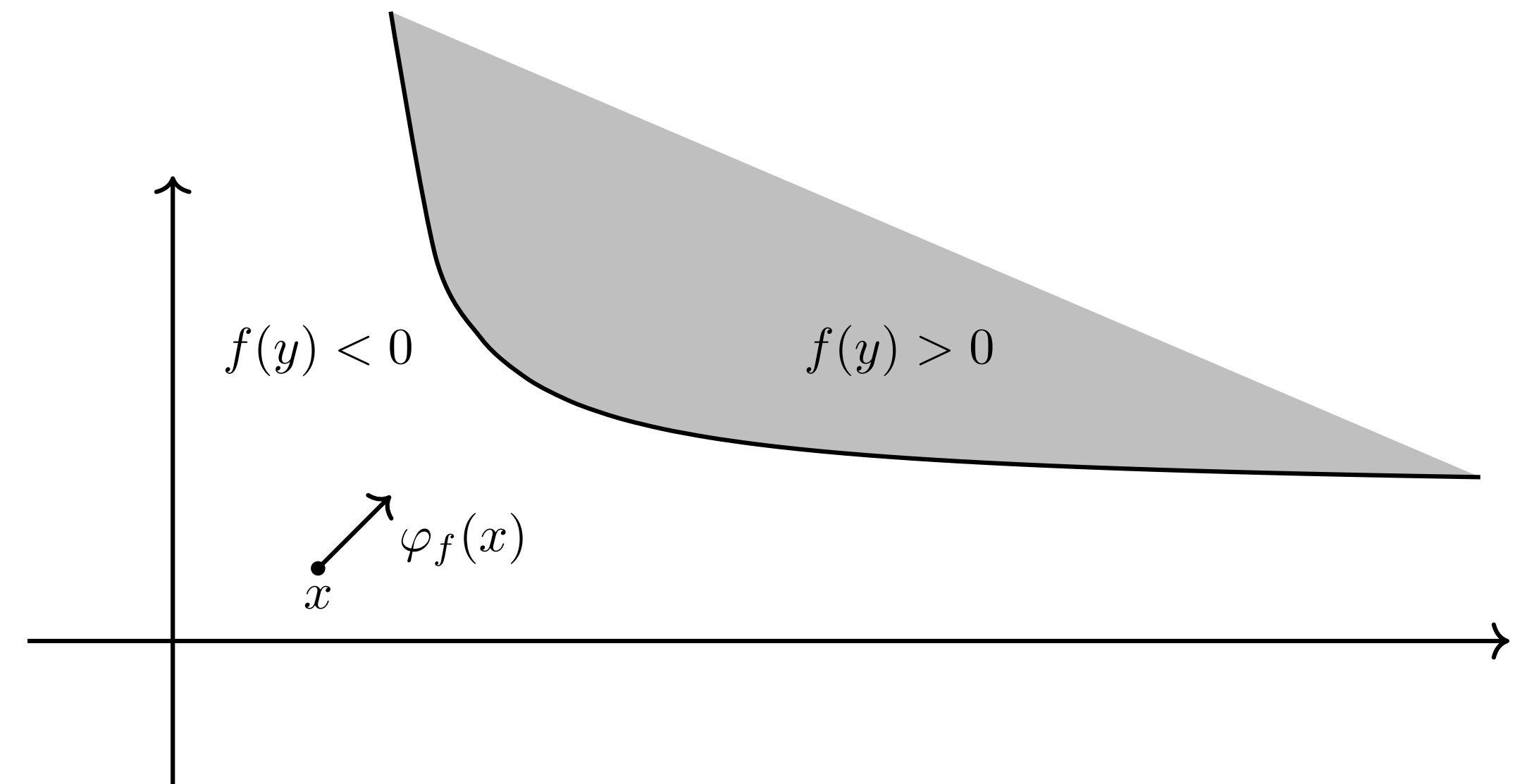


$$\varphi_f(x) = P_U(x) - x$$

Recourse and Robustness is possible sometimes

General case

- ▶ General Utility $u_f(x, y)$
- ▶ $U(x) = \{y \mid u_f(x, y) \geq \tau\}$ become x dependent
- ▶ We need:
 - “Continuity of $U(x)$ ”
 - Projections should exist and be unique



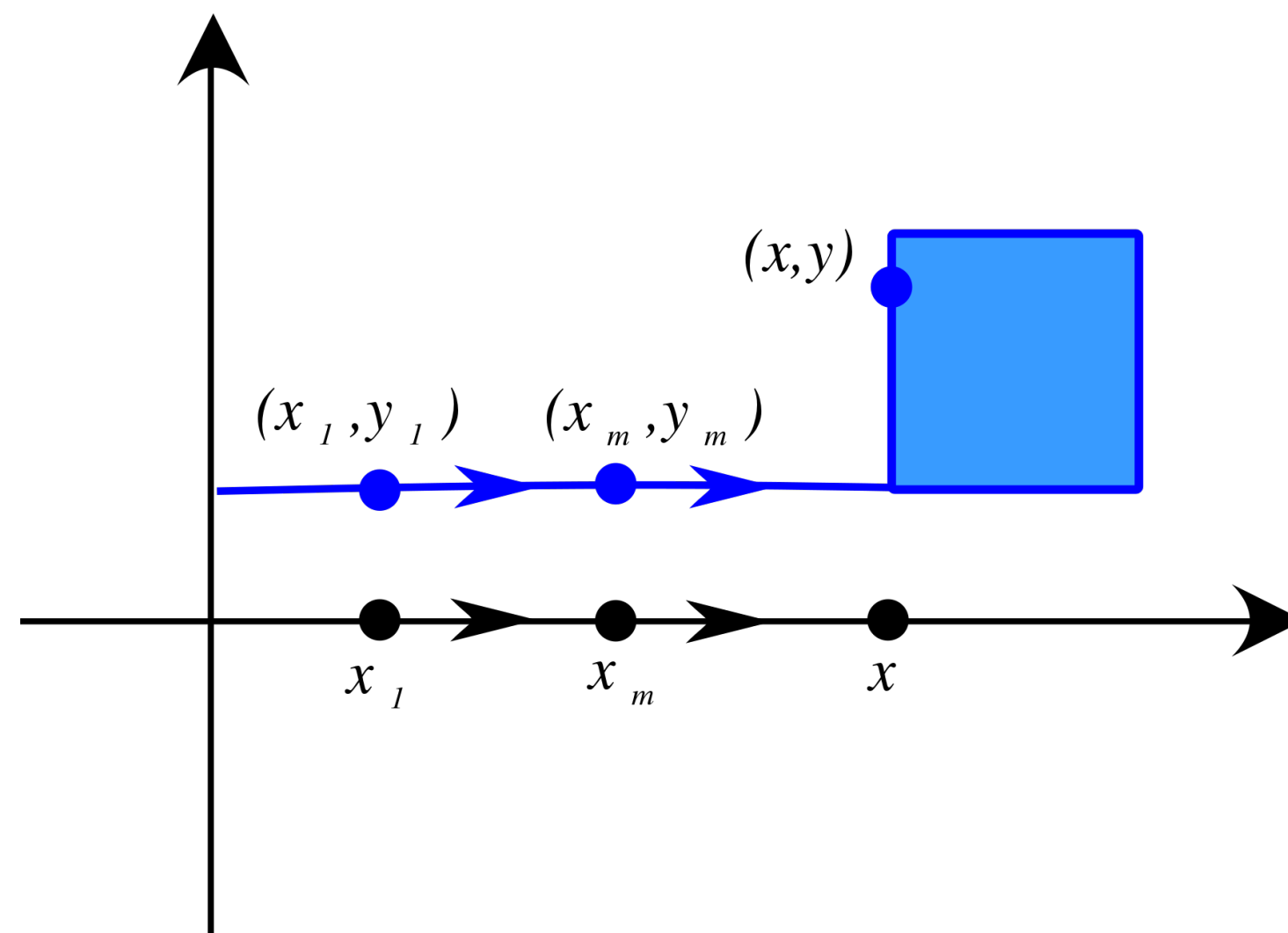
$$\varphi_f(x) = P_U(x) - x$$

Hemi-continuity

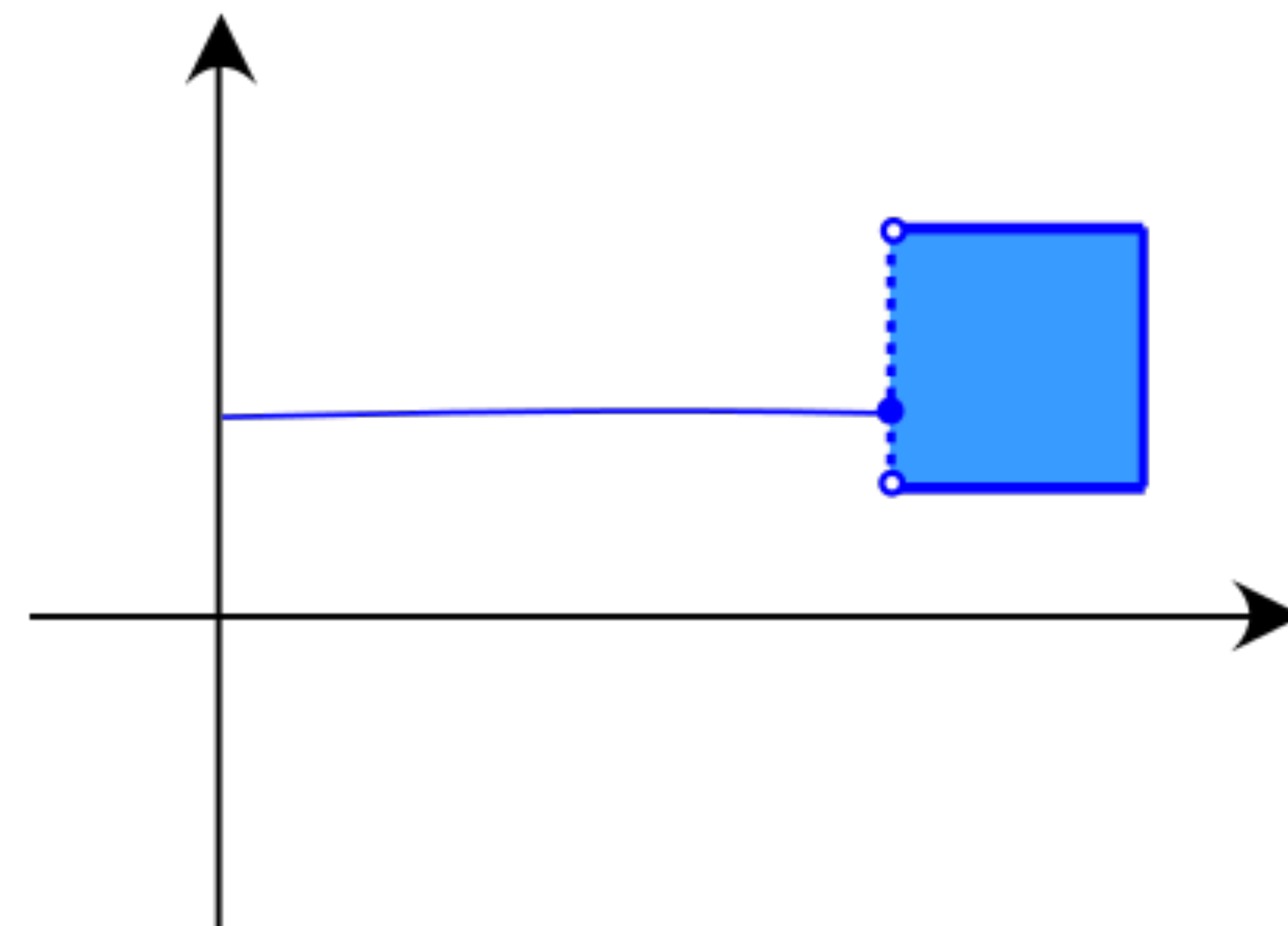
Set-valued function $U: \mathcal{X} \rightarrow 2^{\mathcal{Y}}$:

- ▶ Upper Hemi-continuity: $U(x)$ cannot suddenly explode
- ▶ Lower Hemi-continuity: $U(x)$ cannot suddenly implode

UHC, but not LHC⁴



LHC, but not UHC⁴



Recourse and Robustness is possible sometimes

General case

Theorem

Let $\delta > 0$, $\tau \geq 0$, $f: \mathcal{X} \rightarrow \mathbb{R}$ be a continuous function and $u_f(x, y)$ a utility function with the following properties:

1. For every $x \in \mathcal{X}$, the projection onto $U(x)$ exists and is unique;
2. The set-valued function $U(x)$ is Hemi-continuous and closed.

Then the function given by:

$$\varphi_f(x) = \arg \min_{y \in U(x)} \|x - y\| - x = P_{U(x)}(x) - x$$

Is a recourse sensitive and robust attribution map.

Recourse and Robustness is possible sometimes

General case

Berge's Maximum Theorem

Let $\mathcal{X}, \mathcal{Y} \subseteq \mathbb{R}^d$, assume that:

1. The function $v : \mathcal{X} \times \mathcal{Y} \rightarrow \mathbb{R}$ is a continuous function;
2. The set-valued $U : \mathcal{X} \rightarrow 2^{\mathcal{Y}}$ is semi-continuous, never empty, and attains compact sets.

Then, the parametrized optimization problem $v^*(x) := \inf_{y \in U(x)} v(x, y)$ is continuous and the set-valued solution function

$U^*(x) = \{y \in U(x) \mid v^*(x) = v(x, y)\}$ is UHC and compact-valued

Recourse and Robustness is possible sometimes

General case

Theorem

Let $\delta > 0$, $\tau \geq 0$, $f: \mathcal{X} \rightarrow \mathbb{R}$ be a continuous function and $u_f(x, y)$ a utility function with the following properties:

1. For every $x \in \mathcal{X}$, the projection onto $U(x)$ exists and is unique;
2. The set-valued function $U(x)$ is Hemi-continuous and closed.

Then the function given by:

$$\varphi_f(x) = \arg \min_{y \in U(x)} \|x - y\| - x = P_{U(x)}(x) - x$$

Is a recourse sensitive and robust attribution map.

Proof idea:

- ▶ Berge's Maximum Theorem gives Continuity almost immediately
 - ▶ $v(x, y) = \|x - y\|$
 - ▶ $U(x)$ is not compact, but there are general versions of Berge that deal with this case
- ▶ Check that Recourse sensitivity is satisfied

Full Characterisation in the Single-Feature Case

Attribution methods can

- Provide Recourse
- Be Robust

In the case of *Single Feature Recourse Sensitivity* and L and R are sufficiently disjoint.

Characterisation

Warm up,
One dimensional case

Define

- $L = \{x \in \mathcal{X} \mid \text{there exists some } y \in [x - \delta, x] \text{ with } u_f(x, y) \geq \tau\},$
- $R = \{x \in \mathcal{X} \mid \text{there exists some } y \in [x + \delta, x] \text{ with } u_f(x, y) \geq \tau\}.$

Theorem

Let $\delta, \tau > 0, f: \mathcal{X} \rightarrow \mathbb{R}$ and let u_f be a utility function with $u_f(x, x) < \tau$ for all $x \in \mathcal{X}$. Then, there exists a continuous recourse sensitive attribution method φ_f for f if and only if there exists $\tilde{L} \subseteq L$ and $\tilde{R} \subseteq R$ such that $\tilde{L} \cup \tilde{R} = L \cup R$ and $\tilde{L}$ and $\tilde{R}$ are separated.

Definition

Two sets $A, B \subseteq \mathcal{X}$ are called *separated* if $\text{cl}(A) \cap B = A \cap \text{cl}(B) = \emptyset$

Characterisation

Warm up,
One dimensional case

L

R

Allowed

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Not Allowed

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Conclusion

Summary:

- ▶ There exist f for which recourse sensitivity + robustness is **impossible**, for several machine learning tasks
- ▶ There are cases for which it is **possible**, but they require strong conditions
- ▶ Full Characterisation for Single-Feature case
- ▶ Further extensions in the paper:
 - ▶ Sufficient Conditions for when Recourse and Robustness is possible
 - ▶ Discussion on possible ways around this Impossibility result
 - ▶ Constraints on user actions

Thank you for your attention!

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